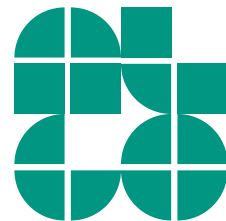


# Algorithms for Graph Visualization

## Introduction to Practical Task

INSTITUT FÜR THEORETISCHE INFORMATIK · FAKULTÄT FÜR INFORMATIK

Marcel Radermacher and Tamara Mchedlidze

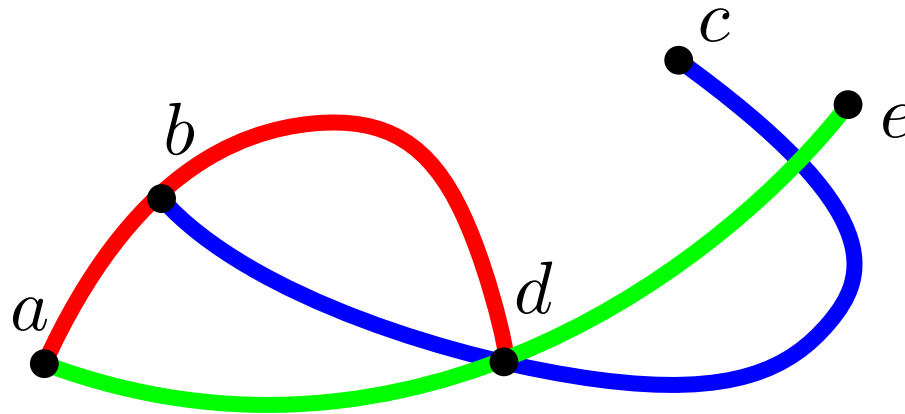




**Definition:**  $H = (V, \mathcal{E})$  a hypergraph.

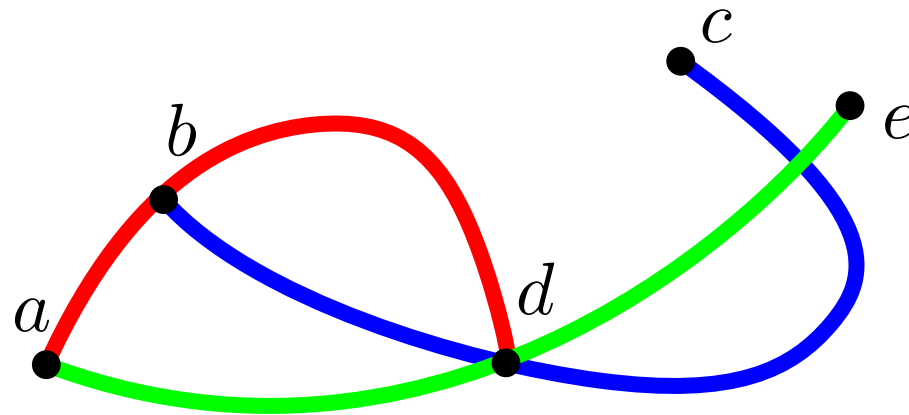
**Line-representation** of  $H$ :

- $V$  is depicted by a set of points on the plane,
- $E$  as a set of curves such that the curve corresponding to  $E \in \mathcal{E}$  passes through all vertices in  $E$ .



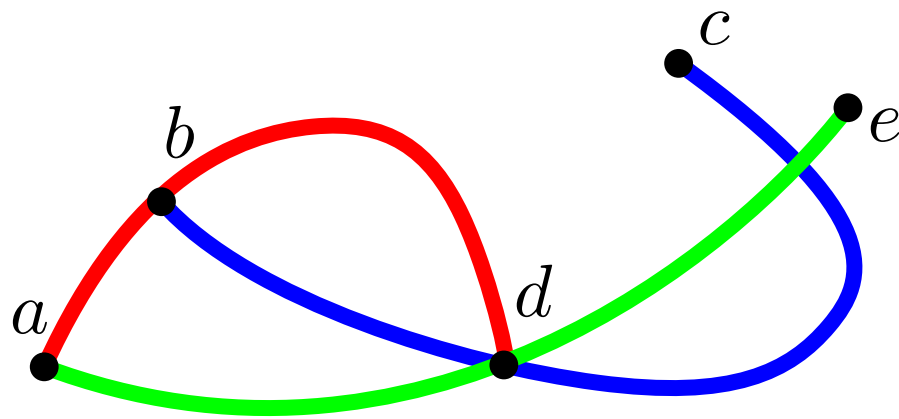
Hypergraph  $H = (\{a, b, c, d, e\}, \{\{a, b, d\}, \{b, c, d\}, \{a, d, e\}\})$

**Your Task:** Heuristic approaches for line-representations

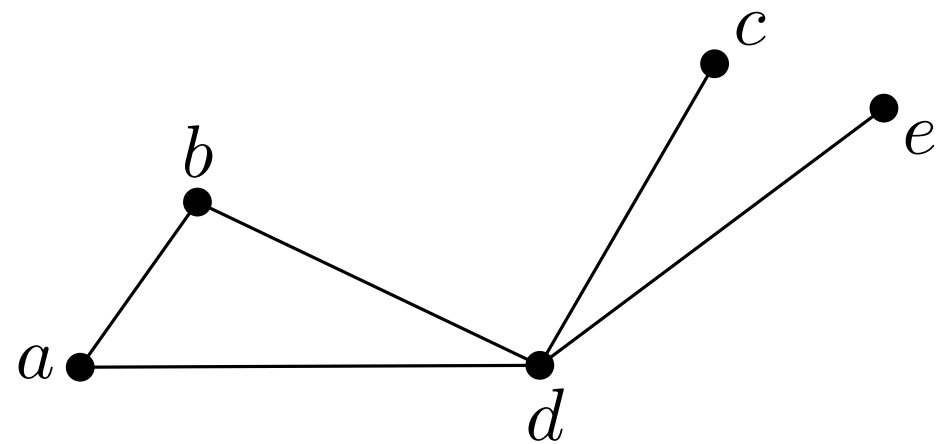


Hypergraph  $H = (\{\{a, b, c, d, e\}, \{\{a, b, d\}, \{b, c, d\}, \{a, d, e\}\})$

- The graph  $G = (V, E)$ ,  $E = \{\text{set of segments connecting two consequent stations}\}$  is called a **path-based support graph** of hypergraph  $H$

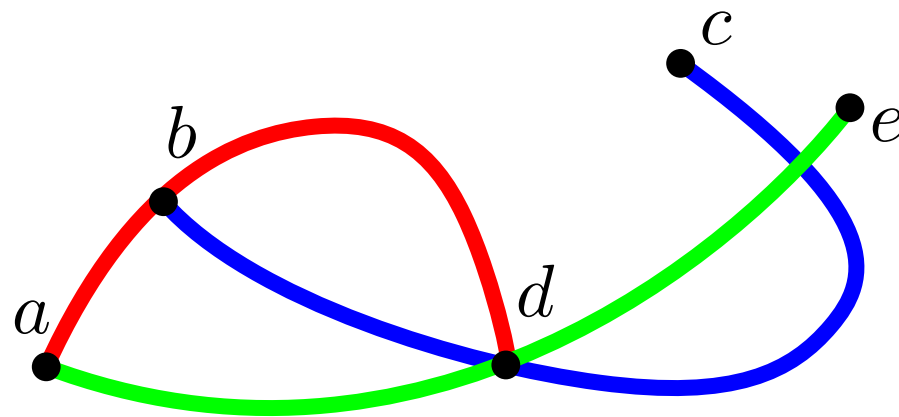


Path-based support of  $H$

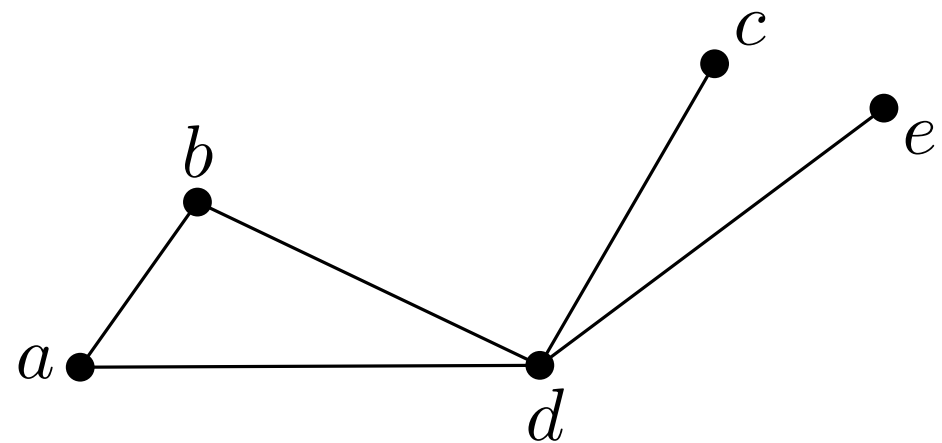


Hypergraph  $H = (\{\{a, b, c, d, e\}, \{\{a, b, d\}, \{b, c, d\}, \{a, d, e\}\})$

- The graph  $G = (V, E)$ ,  $E = \{\text{set of segments connecting two consequent stations}\}$  is called a **path-based support** graph of hypergraph  $H$
- It is **path-based** support, because each hyperedge is represented by a path (not necessarily induced)
- More generally in a **support** graph of  $H$ , each hyperedge induces a connected graph



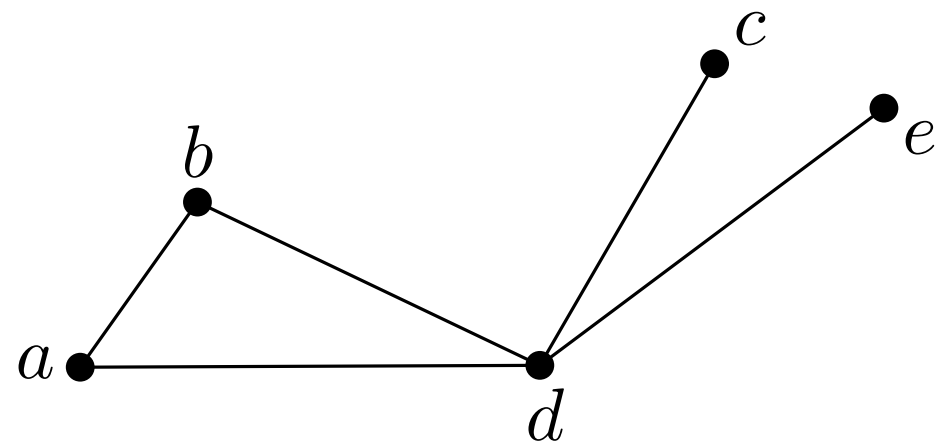
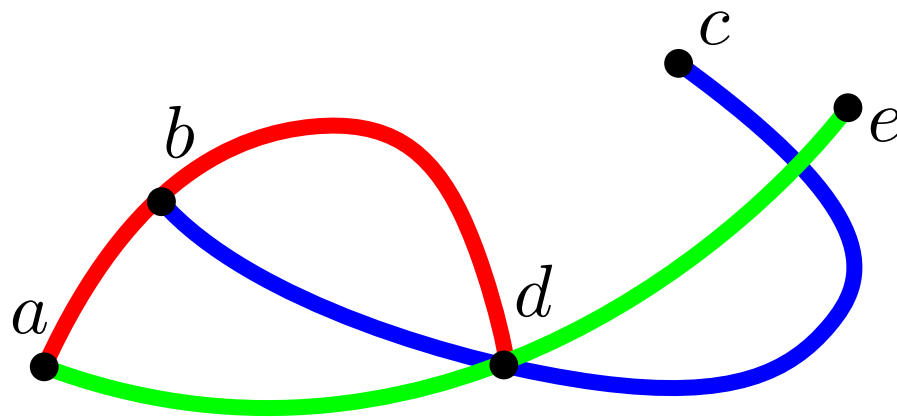
Path-based support of  $H$



Hypergraph  $H = (\{a, b, c, d, e\}, \{\{a, b, d\}, \{b, c, d\}, \{a, d, e\}\})$

- Given a hypergraph  $H$  it is NP-complete to compute a path-based support with the minimum number of edges
- or to decide whether there is a planar path-based support

[Brandes et al., Path-based supports for hypergraphs. J. Disc. Alg., 2012]



Hypergraph  $H = (\{a, b, c, d, e\}, \{\{a, b, d\}, \{b, c, d\}, \{a, d, e\}\})$

## **Your Task:** Heuristic approaches for line-representations

### **Part A:**

- Compute a path-based support, that has a reasonable visualization: not necessarily planar, with minimum edges, etc.
- You can also formalise the problem and study it theoretically.
- Provide a heuristic and implement it.
- Or formally prove some bounds on the performance of the heuristic.



## **Your Task:** Heuristic approaches for line-representations

### **Part B:**

- Draw the path-based support using existing or modified algorithms (e.g. force-directed).
- The target is to draw the graph so that each path is readable.
- How can we formalise the readability?
- What are aesthetic measures?

## **Your Task:** Heuristic approaches for line-representations

### **Part B:**

- Draw the path-based support using existing or modified algorithms (e.g. force-directed).
- The target is to draw the graph so that each path is readable.
- How can we formalise the readability?
- What are aesthetic measures?

### **Part C:** Implement the display the paths.

## **Your Task:** Heuristic approaches for line-representations

### **Part B:**

- Draw the path-based support using existing or modified algorithms (e.g. force-directed).
- The target is to draw the graph so that each path is readable.
- How can we formalise the readability?
- What are aesthetic measures?

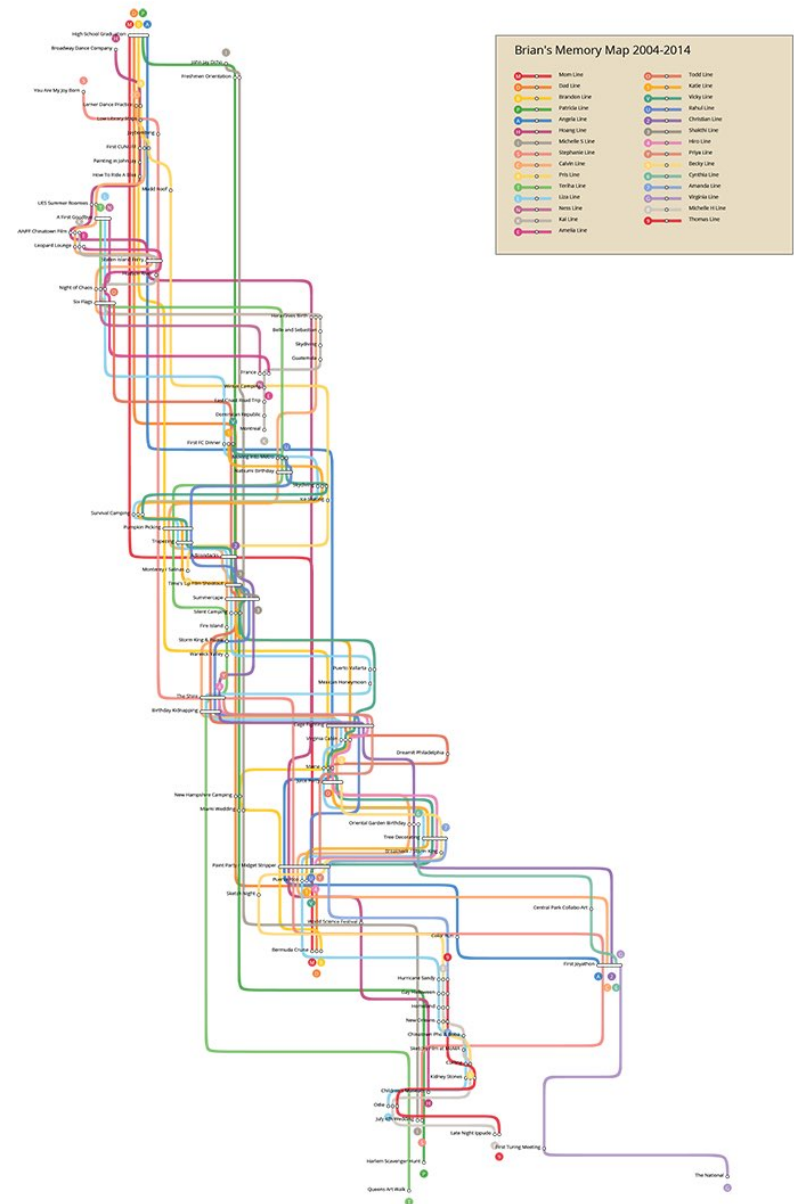
### **Part C:** Implement the display the paths.

### **Options:**

- Give priority to either part A or part B
- Think of an integrated approach

## Building a memory transit map

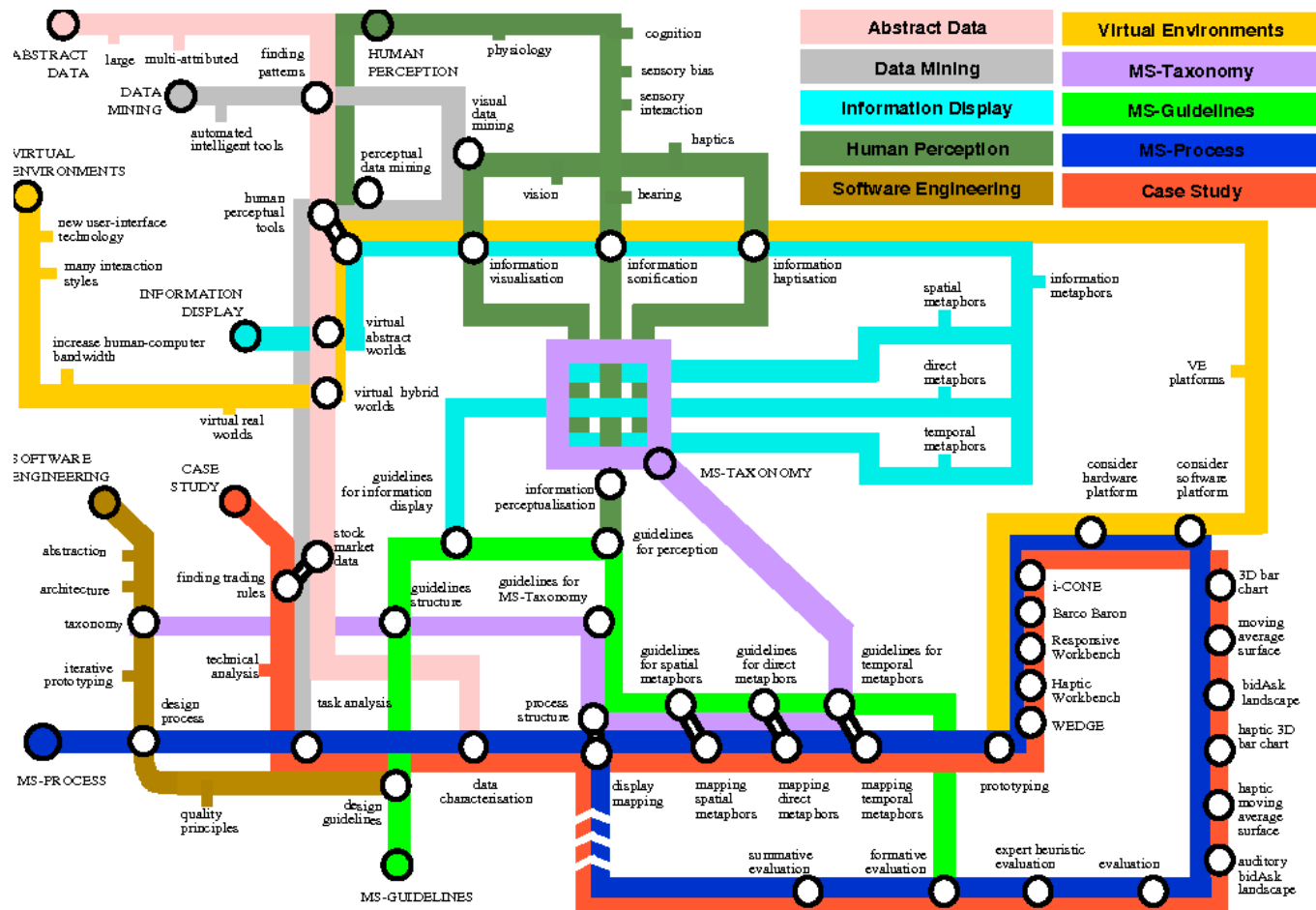
- <http://memoryunderground.com>
- Brian Foo
- The input assumes a sequence of events, i.e. vertices within a hyperedge are ordered



## “Getting to more abstract places using the metro map metaphor”

Keith Nesbitt

InfoVis 2004

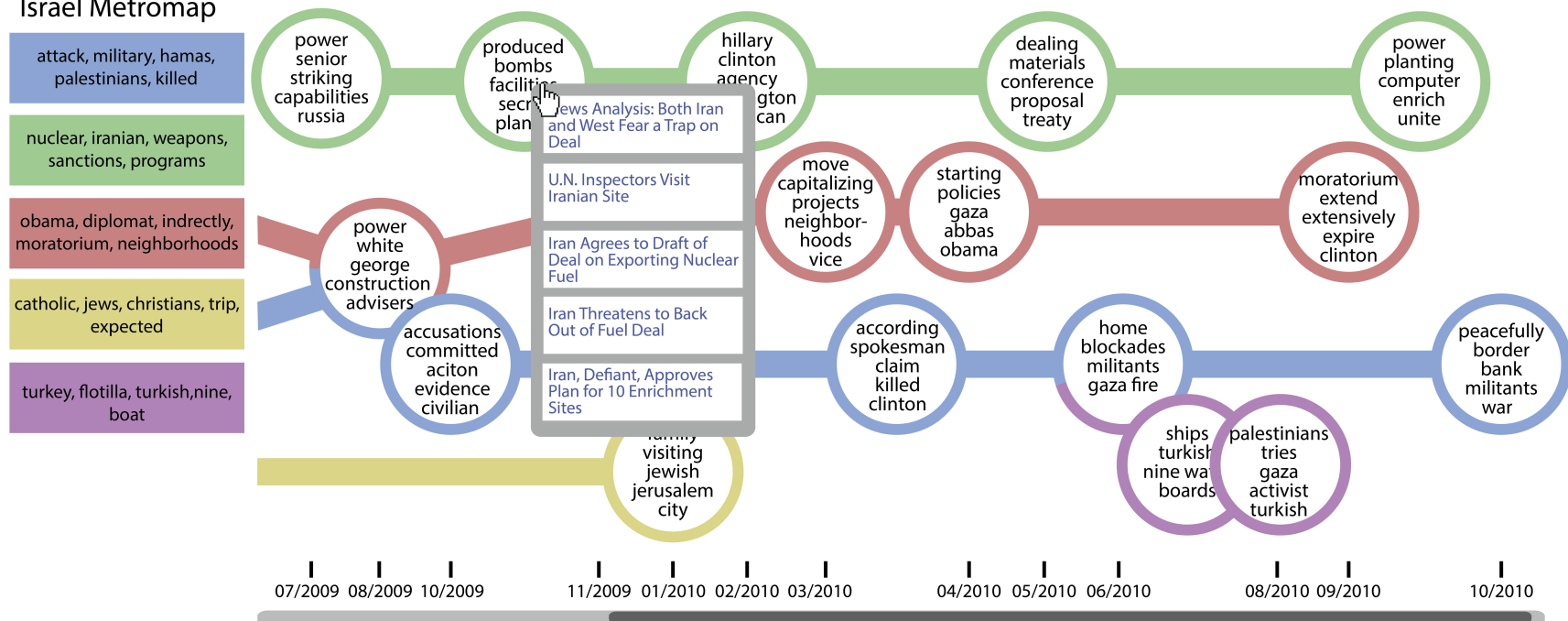


## Metromaps of historical events

“Information Cartography: Creating Zoomable, Large-Scale Maps of Information”

Jure Leskovec et al.  
KDD 2013

Israel Metromap



- “Automatic Layout of Project Plans Using a Metro Map Metaphor”  
Stott et al, InfoVis 2005.
- “A metro map metaphor for guided tours on the Web: the Webwise guided tour system”, Sandvad et al, WWW 2001.