property $P$ :	G is a comparability graph.
property $\overline{P}$ :	$\overline{G}$ is a comparability graph.
property C:	G is a chordal graph.
property $\overline{C}$ :	$\overline{G}$ is a chordal graph.

P	$\overline{P}$	C	$\overline{C}$	graph class
$\checkmark$				comparability graphs
		$\checkmark$		chordal graphs
	$\checkmark$	$\checkmark$		interval graphs
		$\checkmark$	$\checkmark$	split graphs
$\checkmark$	$\checkmark$			permutation graphs
$\checkmark$		$\checkmark$		cycle-free partial orders

Chap.4 Chap.3 Chap.7 Chap.5 Chap.6

## Thm.

For every (undirected) graph G = (V, E) the following are equivalent: (i) G and  $\overline{G}$  are comparability graphs. (ii) There exists a vertex ordering  $\sigma$  of G and without without (iii) There exists an embedding  $V \to \mathbb{R}^2$  such that  $uv \in E$  if and only if  $u_x < v_x \Leftrightarrow u_y < v_y$ 

















segments, intersection

property $P$ :	G is a comparability graph.
property $\overline{P}$ :	$\overline{G}$ is a comparability graph.
property C:	G is a chordal graph.
property $\overline{C}$ :	$\overline{G}$ is a chordal graph.

P	$\overline{P}$	C	$\overline{C}$	graph class
$\checkmark$				comparability graphs
		$\checkmark$		chordal graphs
	$\checkmark$	$\checkmark$		interval graphs
		$\checkmark$	$\checkmark$	split graphs
$\checkmark$	$\checkmark$			permutation graphs
$\checkmark$		$\checkmark$		cycle-free partial orders

Chap.4 Chap.3 Chap.7 Chap.5 Chap.6

## Thm 7.1.

For every graph G = (V, E) the following are equivalent: (i) G is an interval graph. (ii)  $\exists$  vertex ordering  $\sigma$  without (iii) G is chordal and  $\overline{G}$  is a comparability graph. (iv)  $C_4 \not\subseteq_{\text{ind}} G$  and  $\overline{G}$  is a comparability graph. (v) There exists an ordering  $A_1, \ldots, A_x$  of the inclusion-maximal cliques in G such that  $\forall v \in V$  the numbers in  $\{i \mid v \in A_i\}$ are consecutive in  $\{1, \ldots, x\}$ .

Compute  $\sigma_1$  with LexBFS; 1

- Compute  $\sigma_1$  with LexBFS; 1
- **2** Compute  $\sigma_2$  with LexBFS using  $\sigma_1$  as tie breaker;

- Compute  $\sigma_1$  with LexBFS; 1
- Compute  $\sigma_2$  with LexBFS using  $\sigma_1$  as tie breaker; 2
- Compute  $\sigma_3$  with LexBFS using  $\sigma_2$  as tie breaker; 3

- Compute  $\sigma_1$  with LexBFS; 1
- Compute  $\sigma_2$  with LexBFS using  $\sigma_1$  as tie breaker; 2
- Compute  $\sigma_3$  with LexBFS using  $\sigma_2$  as tie breaker; 3
- Compute  $\sigma_4$  with LexBFS using  $\sigma_3$  as tie breaker; 4

- Compute  $\sigma_1$  with LexBFS; 1
- Compute  $\sigma_2$  with LexBFS using  $\sigma_1$  as tie breaker;
- Compute  $\sigma_3$  with LexBFS using  $\sigma_2$  as tie breaker; 3
- Compute  $\sigma_4$  with LexBFS using  $\sigma_3$  as tie breaker; 4
- **Return** whether  $\sigma_4$  contains forbidden pattern; 5