
Input : graph $G = (V, E)$, vertex ordering σ .

Output : true, if σ PES, false otherwise.

```
1  for each vertex  $v$  do  $A(v) \leftarrow \emptyset$ ;  
2  for  $i \leftarrow 1$  to  $n - 1$  do  
3       $v \leftarrow \sigma(i)$ ;  
4       $X \leftarrow \{x \in \text{Adj}(v) \mid \sigma(v) < \sigma(x)\}$ ;  
5      if  $X = \emptyset$  then go to line 8;  
6       $u \leftarrow \text{argmin}\{\sigma(x) \mid x \in X\}$ ;  
7      add  $X - \{u\}$  to  $A(u)$ ;  
8      if  $A(v) - \text{Adj}(v) \neq \emptyset$  then  
9          | return false;  
10     end if  
11 end for  
12 return true;
```

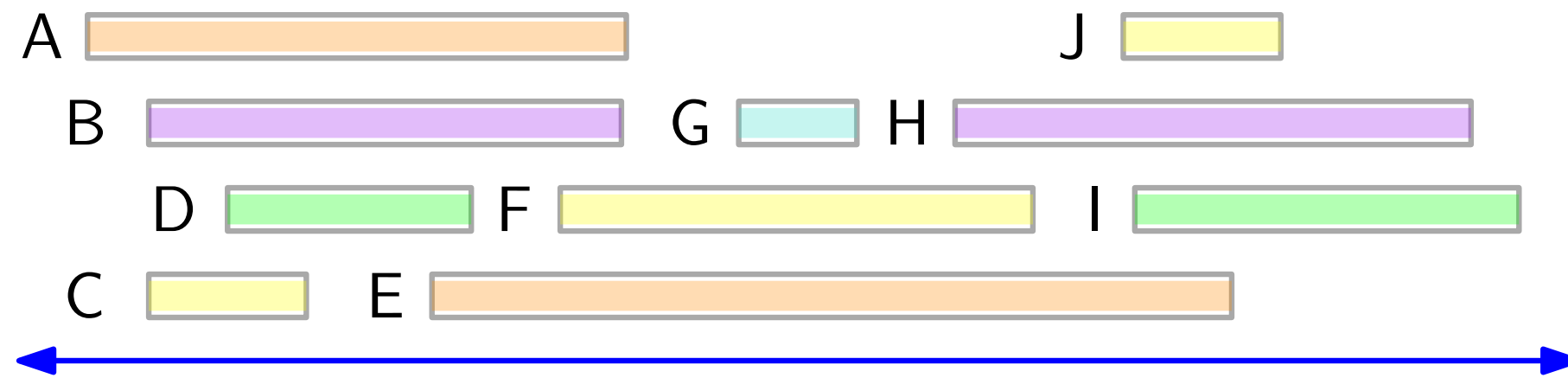
Algorithm 3 : Test for perfect elimination scheme

Input : lists $\text{Adj}(v)$, $A(v)$.

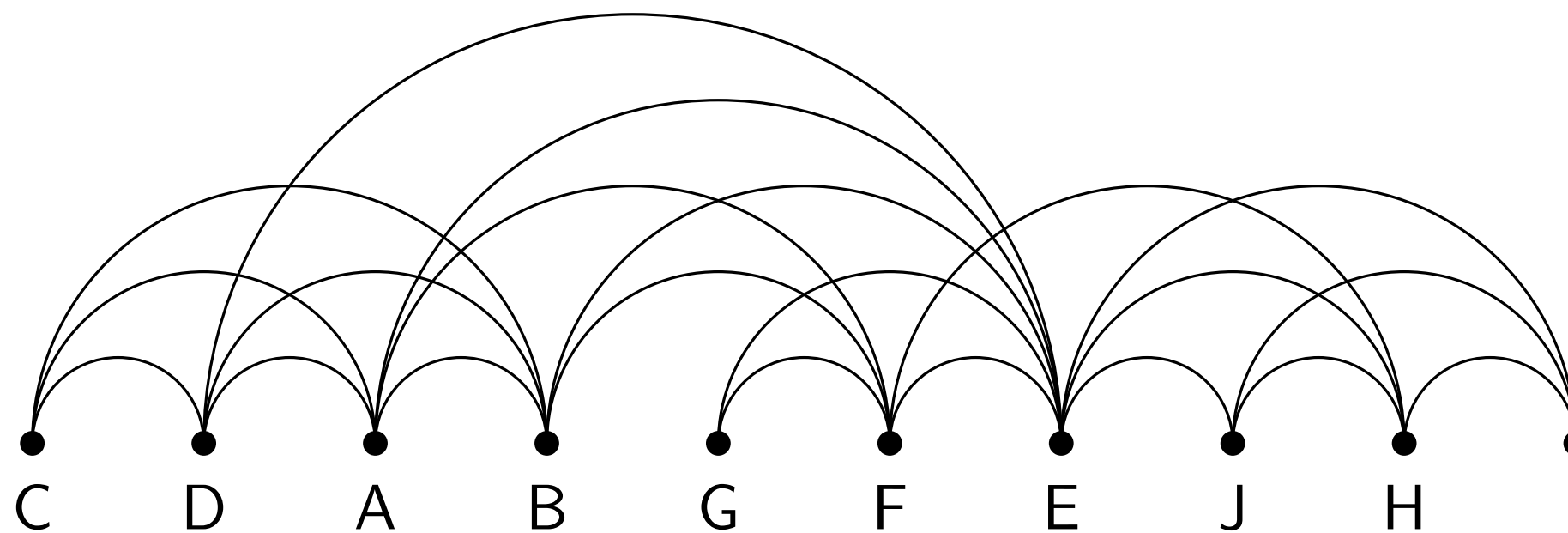
Output : true, if $A(v) - \text{Adj}(v) \neq \emptyset$, false otherwise.

```
1  for  $w \in \text{Adj}(v)$  do  $\text{Test}(w) \leftarrow \text{true};$ 
2  for  $w \in A(v)$  do
3      if  $\text{Test}(w) = \text{false}$  then
4          return true;
5      end if
6  end for
7  for  $w \in \text{Adj}(v)$  do  $\text{Test}(w) \leftarrow \text{false};$ 
8  return false;
```

Algorithm 4 : Test for $A(v) - \text{Adj}(v) \neq \emptyset$ in line 8



For **interval graphs** the **left-to-right ordering of right endpoints** in any interval representation gives a **PES**.



Input : chordal graph $G = (V, E)$.

Output : clique C and coloring ϕ .

```
1  compute with LexBFS a PES  $\sigma$  of  $G$ ;  
2   $C \leftarrow \emptyset, \phi \leftarrow 0$ ;  
3  for  $i \leftarrow n$  to 1 do  
4       $v \leftarrow \sigma(i)$ ;  
5       $X_v \leftarrow \text{Adj}(v) \cap \{\sigma(i+1), \dots, \sigma(n)\}$ ;  
6       $\phi(v) \leftarrow \min(\mathbb{N} - \{\phi(w) \mid w \in X_v\})$ ;  
7      if  $|C| < |X_v + \{v\}|$  then  
8           $C \leftarrow X_v + \{v\}$ ;  
9      end if  
10 end for  
11 return  $C$  and  $\phi$ ;
```

Algorithm 5 : Compute $\omega(G)$ and $\chi(G)$

Input : chordal graph $G = (V, E)$.

Output : independent set U and clique cover ψ .

```
1  compute with LexBFS a PES  $\sigma$  of  $G$ ;
2   $U \leftarrow \emptyset, \psi \leftarrow 0$ ;
3  for  $i \leftarrow 1$  to  $n$  do
4       $v \leftarrow \sigma(i), X_v \leftarrow \text{Adj}(v) \cap \{\sigma(i+1), \dots, \sigma(n)\}$ ;
5      if  $\psi(v) = 0$  then
6           $U \leftarrow U + \{v\}$ ;
7          for  $w \in X_v + \{v\}$  do
8               $\psi(w) \leftarrow |U|$ ;
9          end for
10     end if
11 end for
12 return  $U$  and  $\psi$ ;
```

Algorithm 6 : Compute $\alpha(G)$ and $\kappa(G)$
