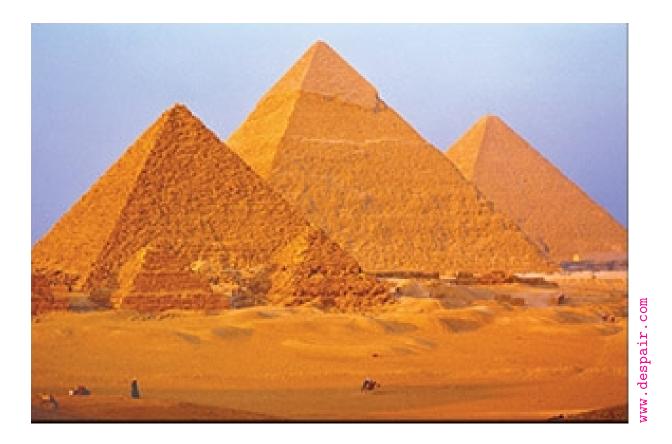
#### **Introduction to Spring Embedder Layouts**



Achievement: You can do anything you set your mind to when you have vision, determination, and an endless supply of expendable labor.

## **Overview**

- Motivation
- Spring Embedder
- Variations

### **Problem: Finding General Layouts**

Problem: How can we determine layouts for general graphs without

## **Problem: Finding General Layouts**

Problem: How can we determine layouts for general graphs without

- having structural properties
- preprocessing (to find structural properties)
- solving NP-hard problems

that are

## **Problem: Finding General Layouts**

Problem: How can we determine layouts for general graphs without

- having structural properties
- preprocessing (to find structural properties)
- solving NP-hard problems

that are

- robust
- flexible
- easy to understand.

#### **Solution: Physical Analogies**

in physics:

- models consist of object and interactions (among them)
- stable configurations (instances) are those with minimal energie levels

### **Solution: Physical Analogies**

in physics:

- models consist of object and interactions (among them)
- stable configurations (instances) are those with minimal energie levels

for layout algorithms:

- nodes correspond to (physical) objects
- edges correspond to interactions
- (good?) layouts correspond to stable configurations

## **Spring-Embedder**

spring model:

- node are small balls with electrical charge (same sign)
- edges are springs with given constant (ideal length)
- nodes repel each others (repulsive force)
- edges cannot be arbitrary long (attractive force)

## **Spring-Embedder (2)**

- $\bullet$  coordinates  $p_v$  for each node v
- lengths  $l_e$  for each edge e

$$f_{\mathsf{rep}}(u,v) := \frac{c_1}{\|p_v - p_u\|^2} \cdot \overrightarrow{p_u p_v}$$

$$f_{\mathsf{spring}}(u,v) := c_2 \cdot \log \frac{\|p_u - p_v\|}{l_e} \cdot \overrightarrow{p_u p_v} \qquad \text{for } (u,v) = e \in E$$

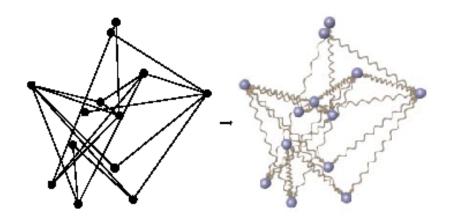
# **Spring-Embedder (3)**

algorithmic approach:

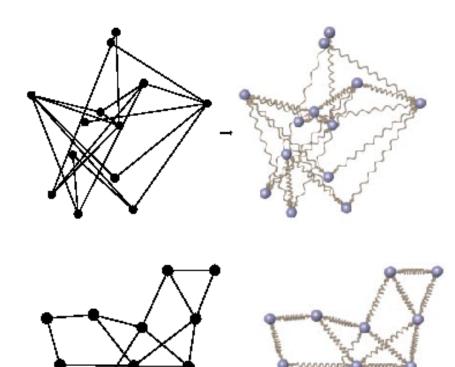
- choose a random placement (for each node)
- iterate
  - calculate for each node v its force vector F(v)
  - move each node  $\boldsymbol{v}$  according to its force vector

$$p_v \leftarrow p_v + \delta \cdot F(v)$$

# **Spring-Embedder (4)**



# **Spring-Embedder (4)**



Carling and the second

#### Variation [Fruchtermann, Reingold]

• repulsive force:

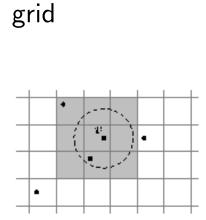
$$f_{\mathsf{rep}}(u,v) := \frac{l_{uv}^2}{\|p_u - p_v\|} \cdot \overrightarrow{p_u p_v}$$

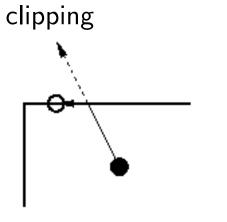
• attractive force:

$$f_{\mathsf{attr}}(u,v) := \frac{\|p_u - p_v\|^2}{l_e} \cdot \overrightarrow{p_v p_u} \qquad \text{for } (u,v) = e \in E$$

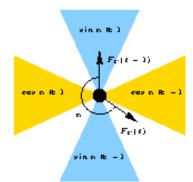
advantage: 'spring' force is super linear in *l* (better convergence)

## Variations





rotation



- time dependency
- gravitational forces
- approximation of forces
- multi-level approaches