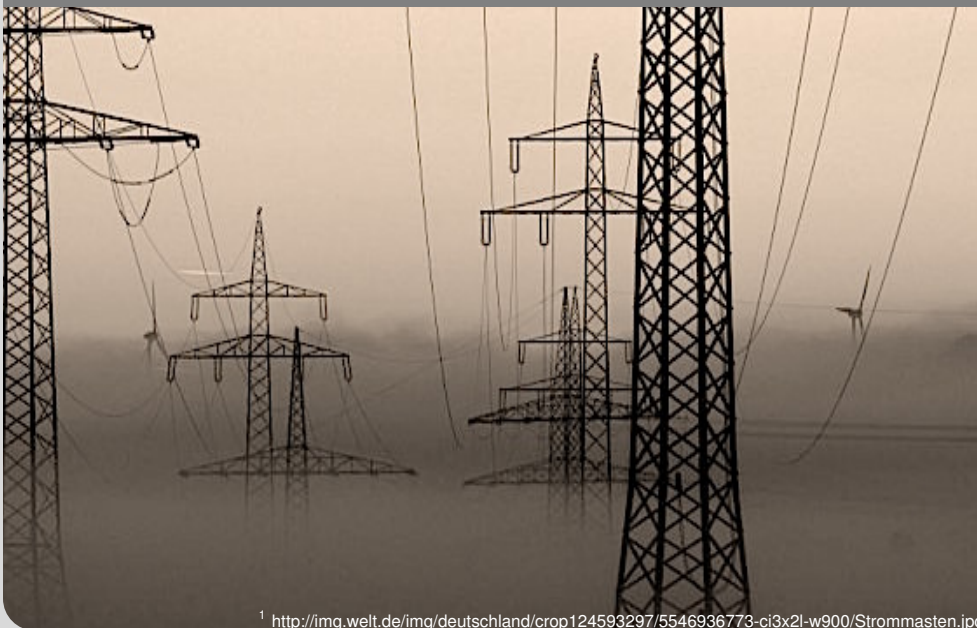
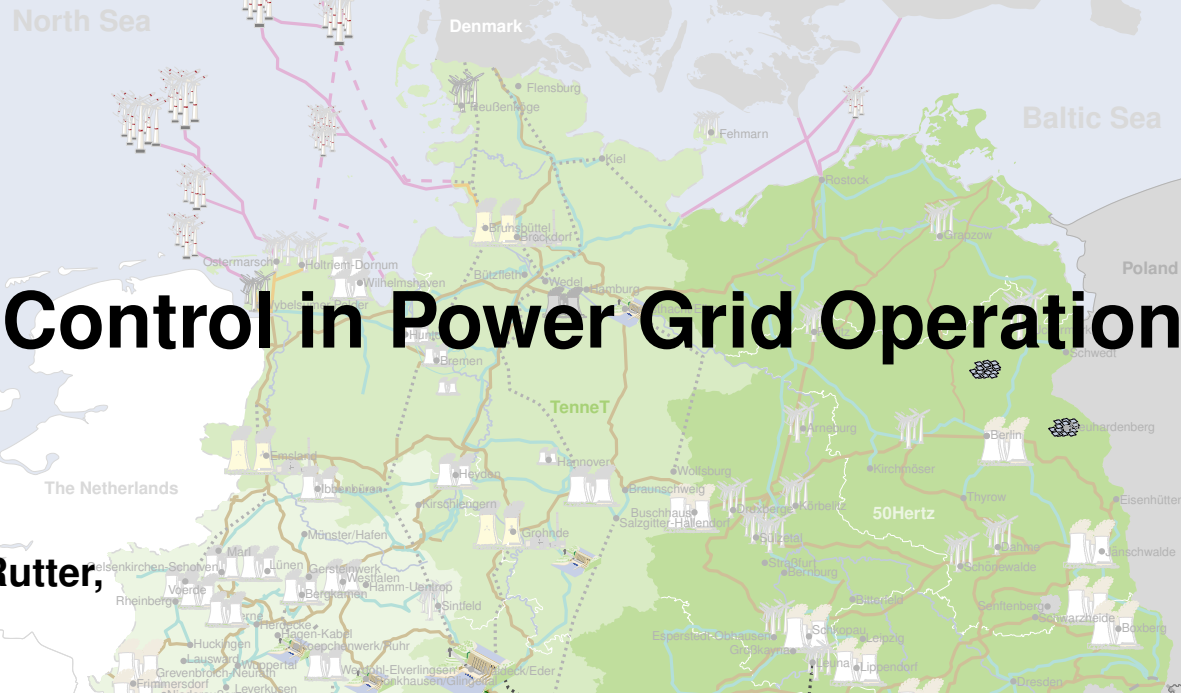


Towards Realistic Flow Control in Power Grid Operation

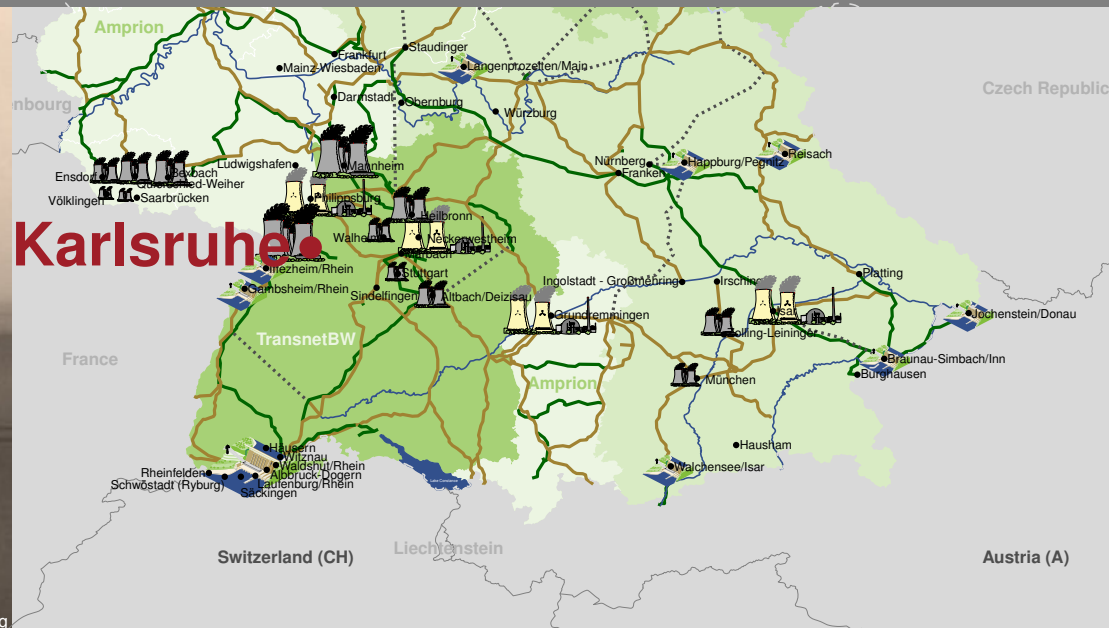
Energy Informatics · Nov 13, 2015

Tamara Mchedlidze, Martin Nöllenburg, Ignaz Rutter,
Dorothea Wagner and Franziska Wegner

INSTITUTE OF THEORETICAL INFORMATICS · ALGORITHMICS GROUP

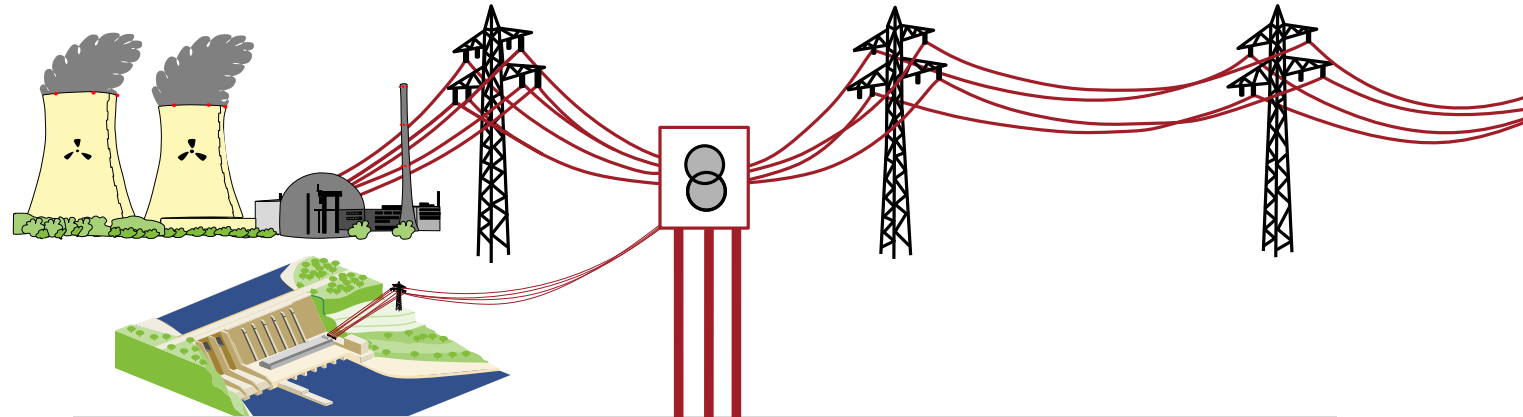


¹ <http://img.welt.de/img/deutschland/crop124593297/5546936773-ci3x2l-w900/Strommasten.jpg>

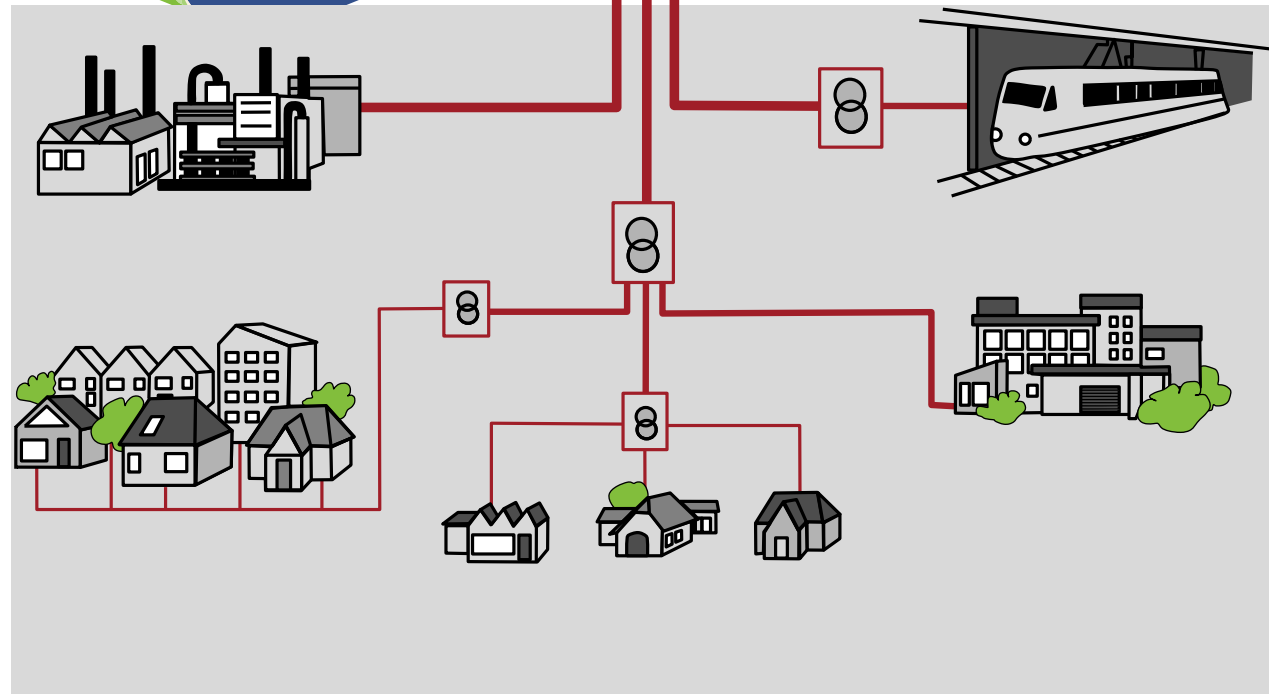


Recent Development in Power Grids

PRODUCER



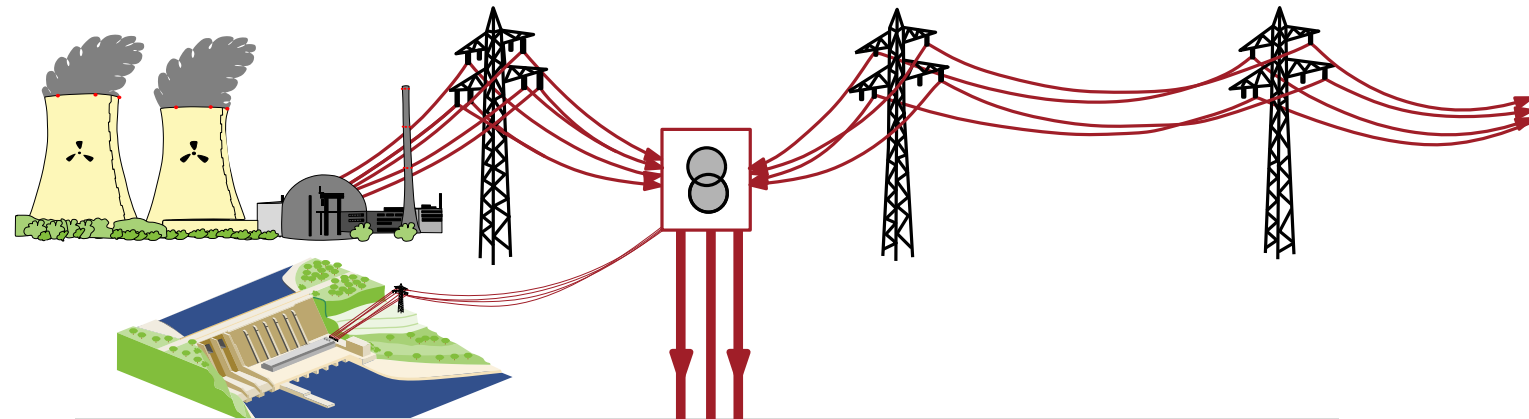
POWER GRID



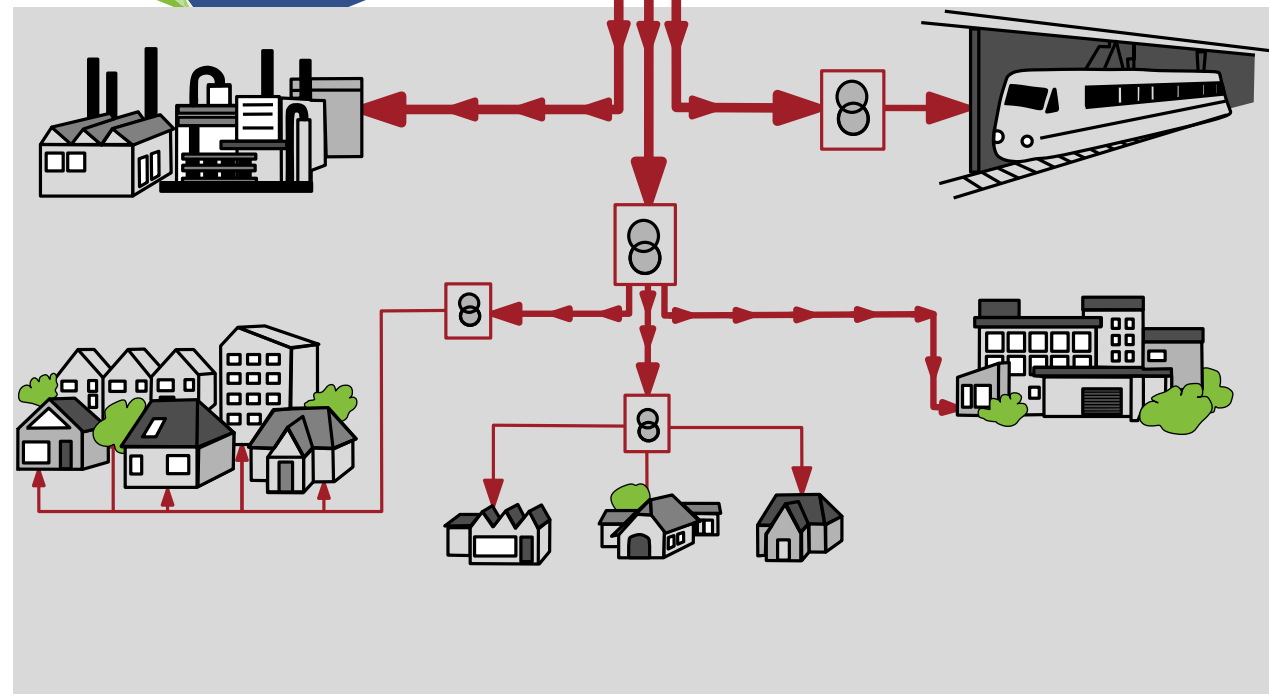
CONSUMER

Recent Development in Power Grids

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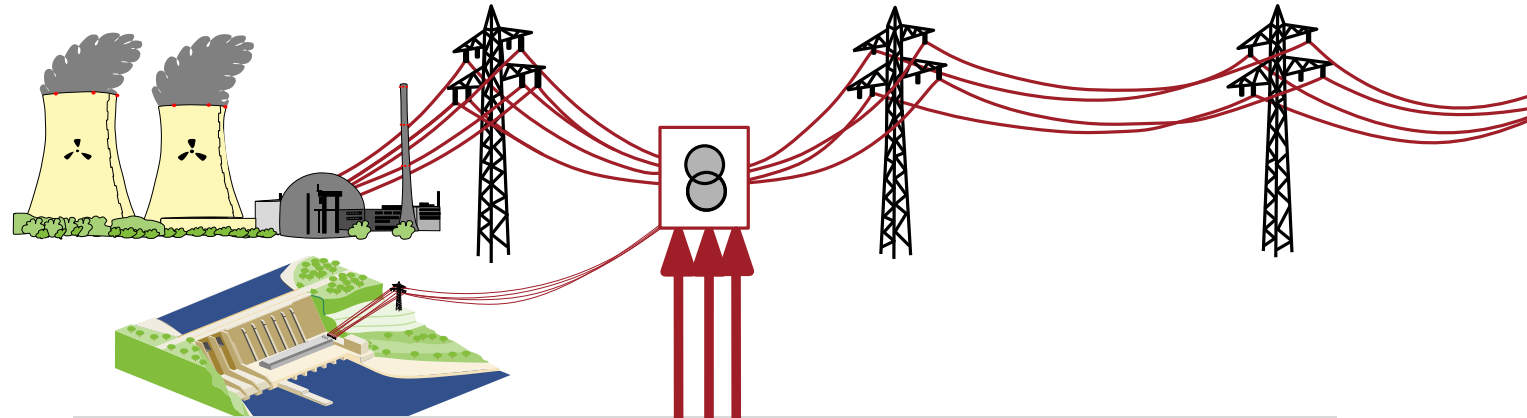
POWER GRID



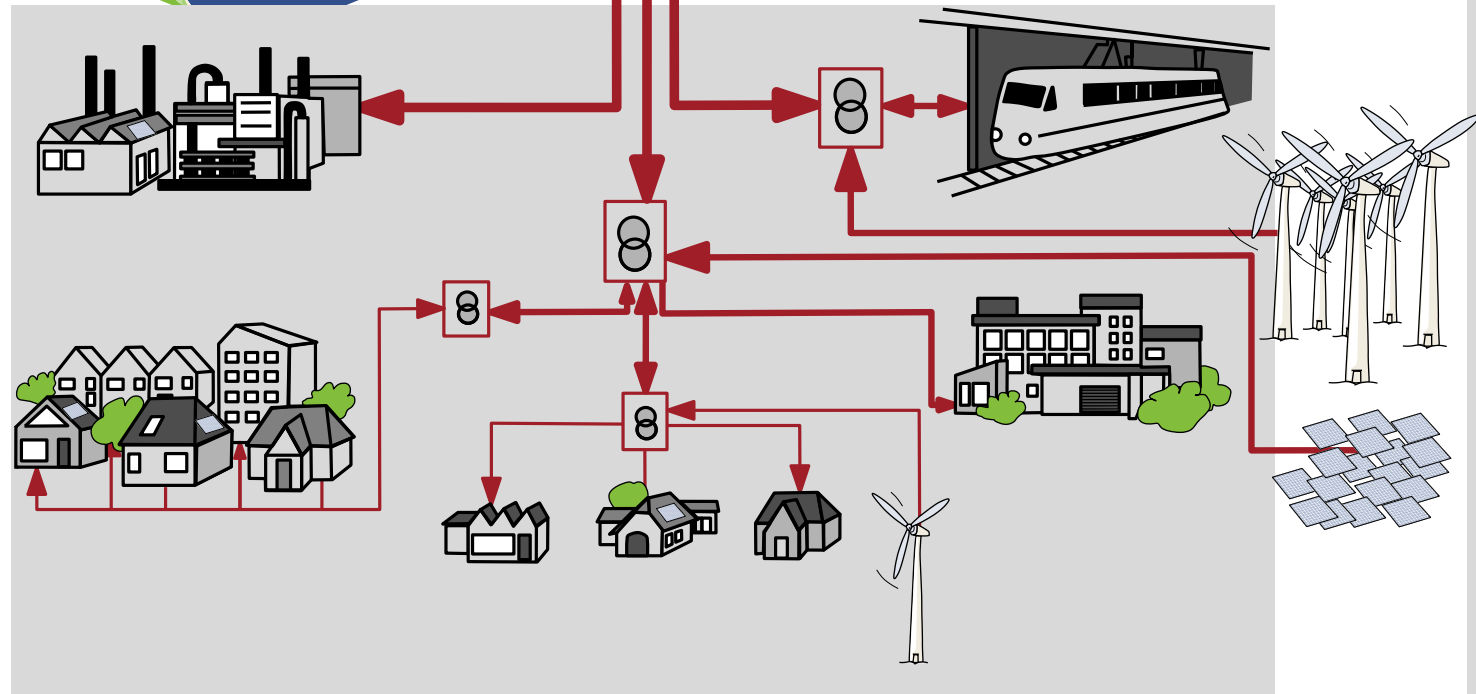
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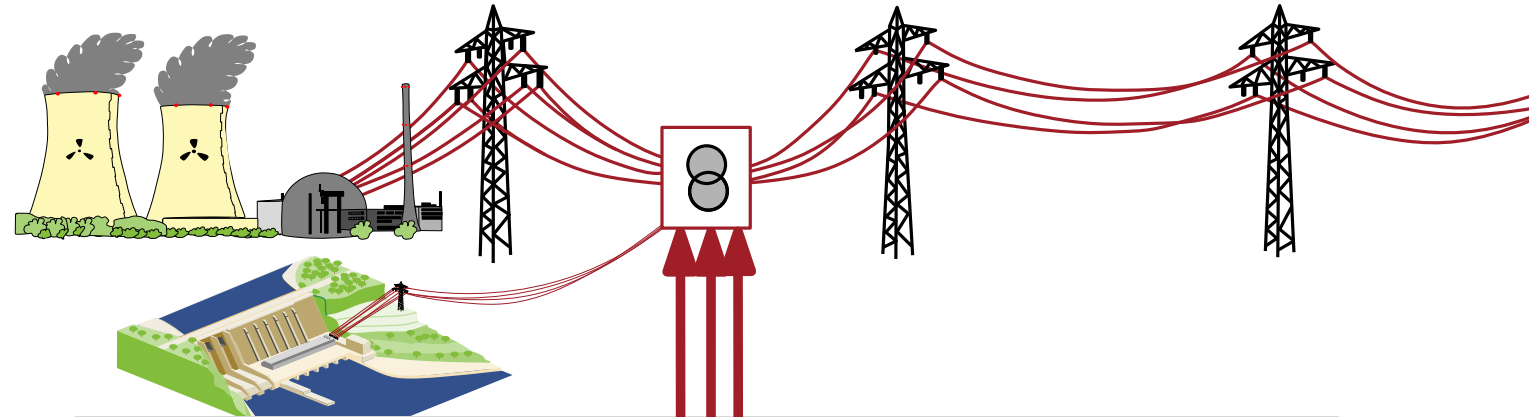
POWER GRID



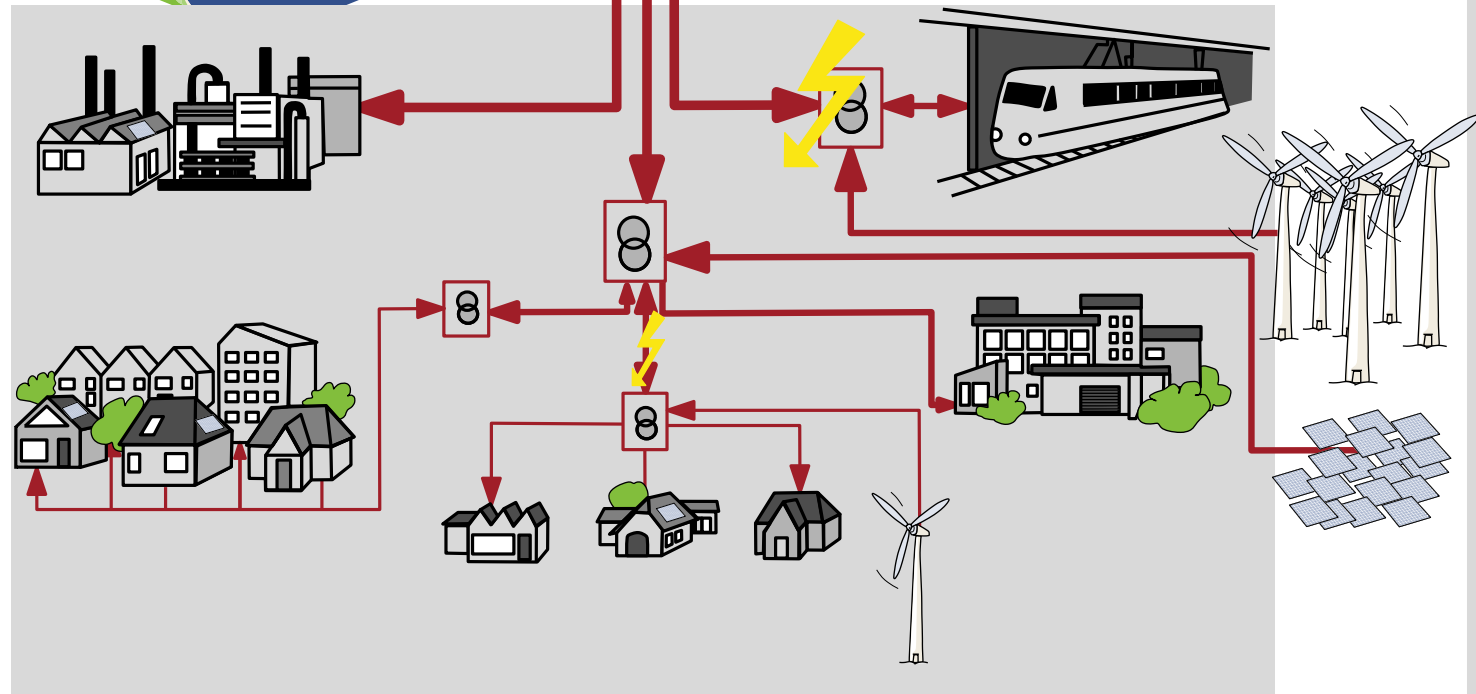
PROSUMER

Recent Development in Power Grids

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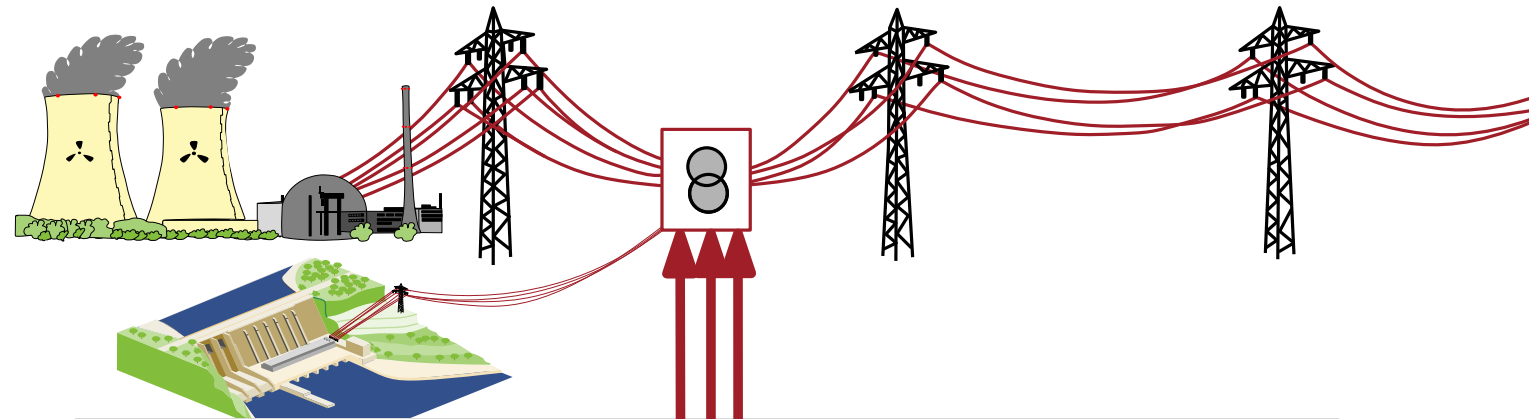
POWER GRID



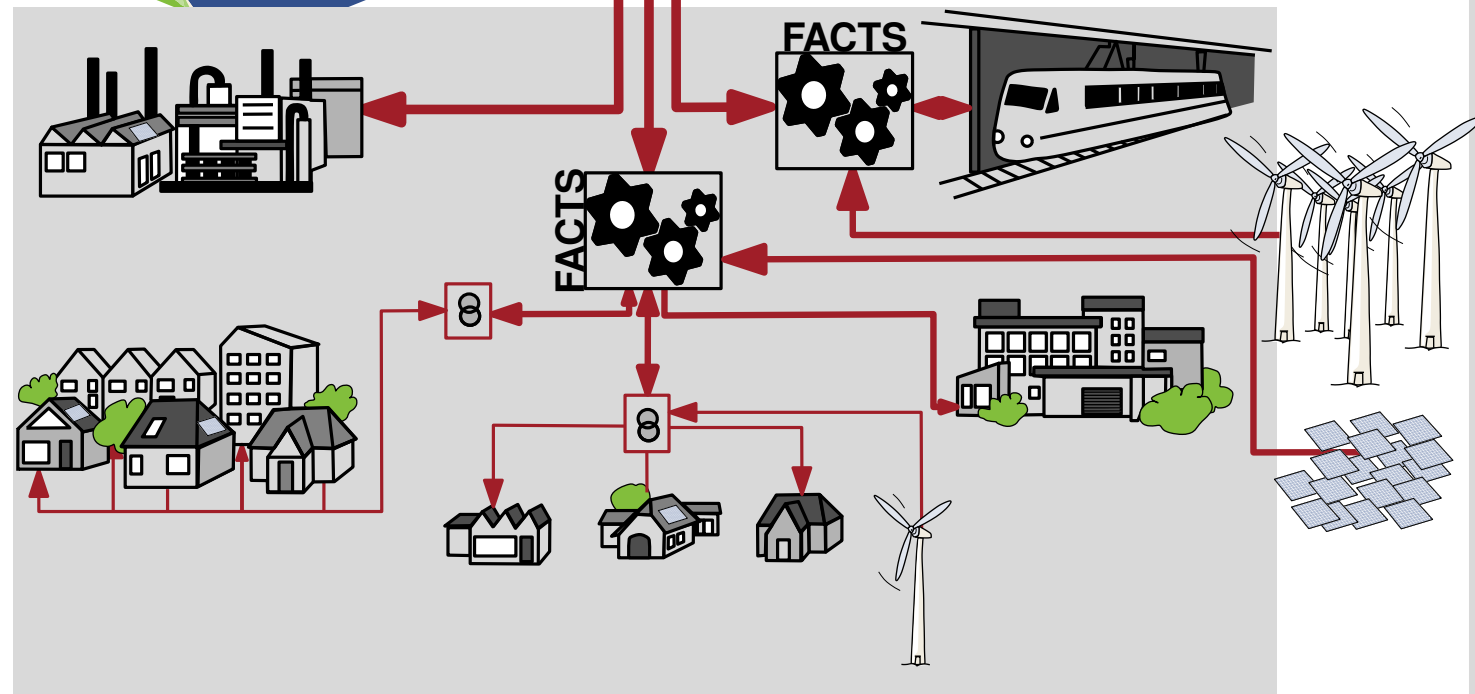
PROSUMER

Recent Development in Power Grids

PRODUCER



POWER GRID



PROSUMER

Challenges

- Increasingly distributed energy production
 - Independent power producers
 - Volatile power flows and flow directions
- ⇒ Operating the power grid gets more demanding

Strategies to cope with the challenges

- Network expansion
- Investment in advanced control units (e.g. FACTS) for better utilization of existing grid

Problem of Power Grid Operator

Given:

- Power grid with parameters

Find:

- Valid operation point (respecting thermal branch limits) for power grid with control units at selected branches
- Energy production of each power generator

Goals:

- Minimize production cost (similar to OPF)
 - Minimize branch losses
- } operation cost

How may we simplify the power grid operator's work?

Problem of Power Grid Operator

Given:

- Power grid with parameters

Find:

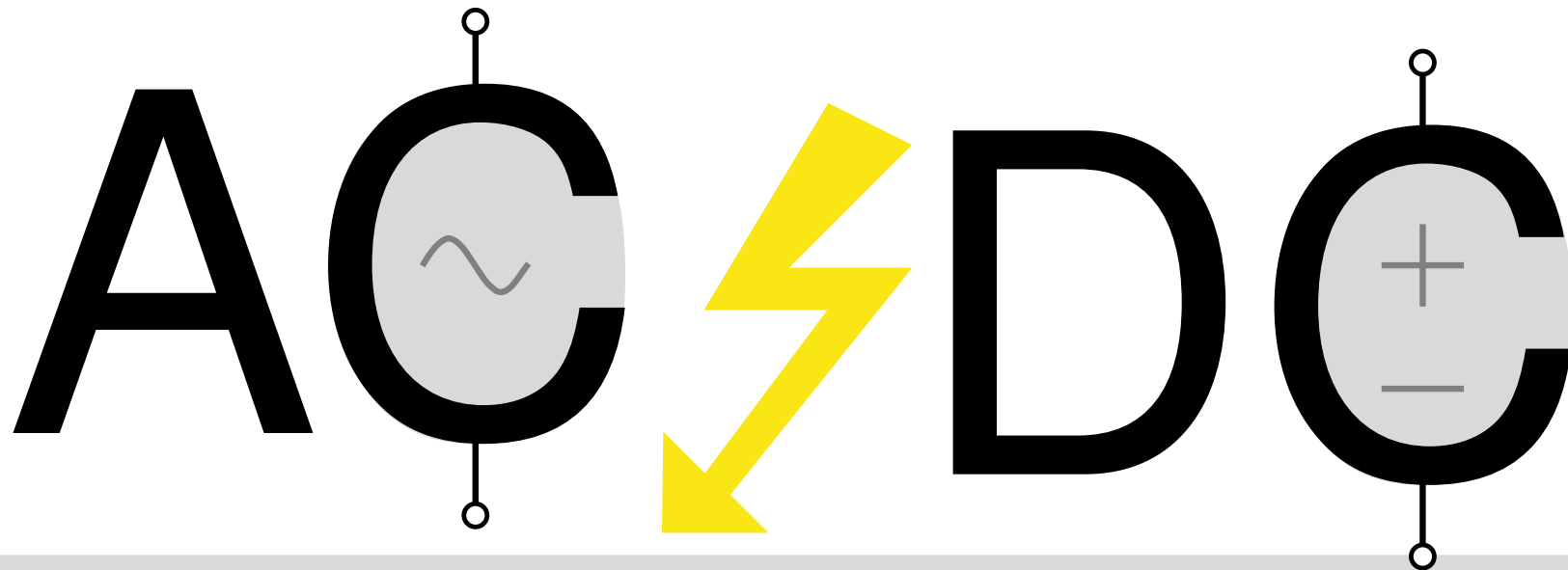
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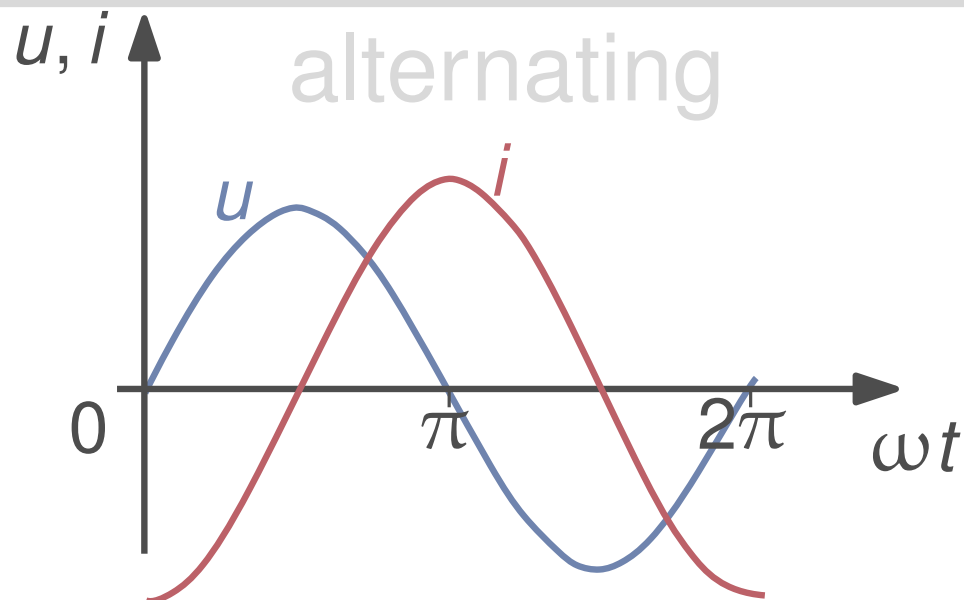
- Minimize production cost (similar to OPF)
 - Minimize branch losses
- } operation cost

How may we simplify the power grid operator's work?

⇒ Place FACTS to enhance controllability.



DC-based Flow Models



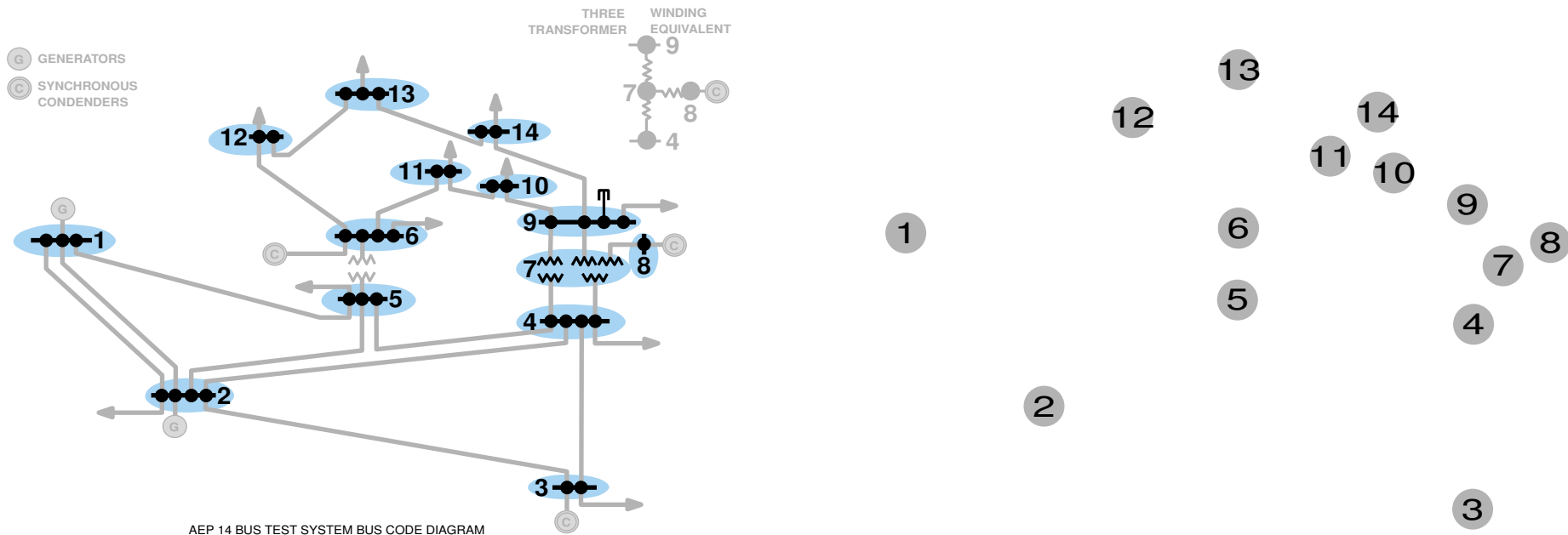
Straight-forward transformation:

- Power grid \rightarrow graph $G = (V, E)$

Graph Model

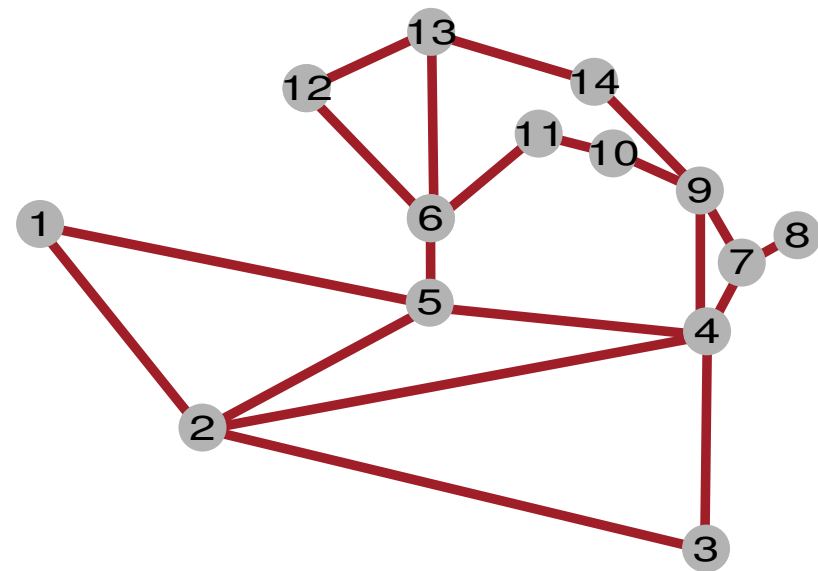
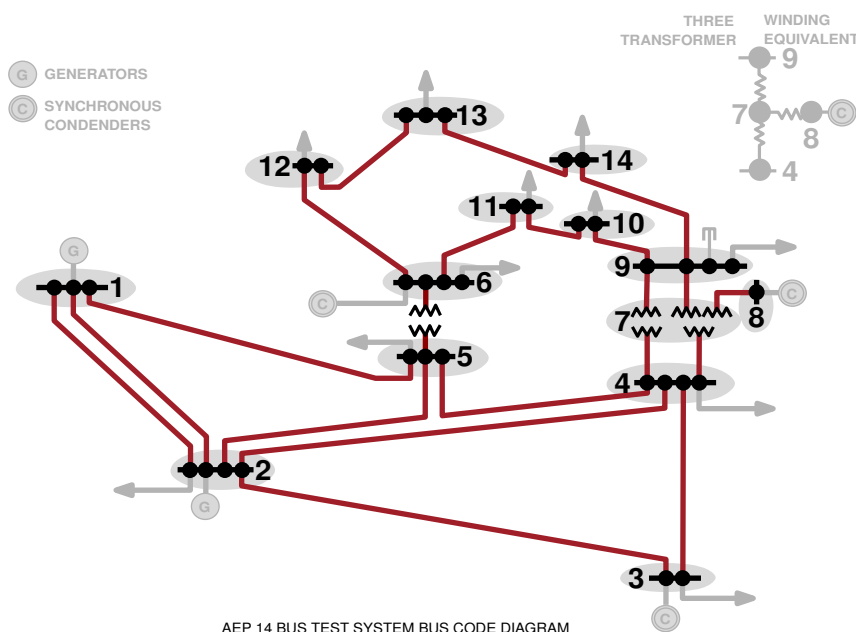
Straight-forward transformation:

- Power grid \rightarrow graph $G = (V, E)$
- Buses \rightarrow vertex set V



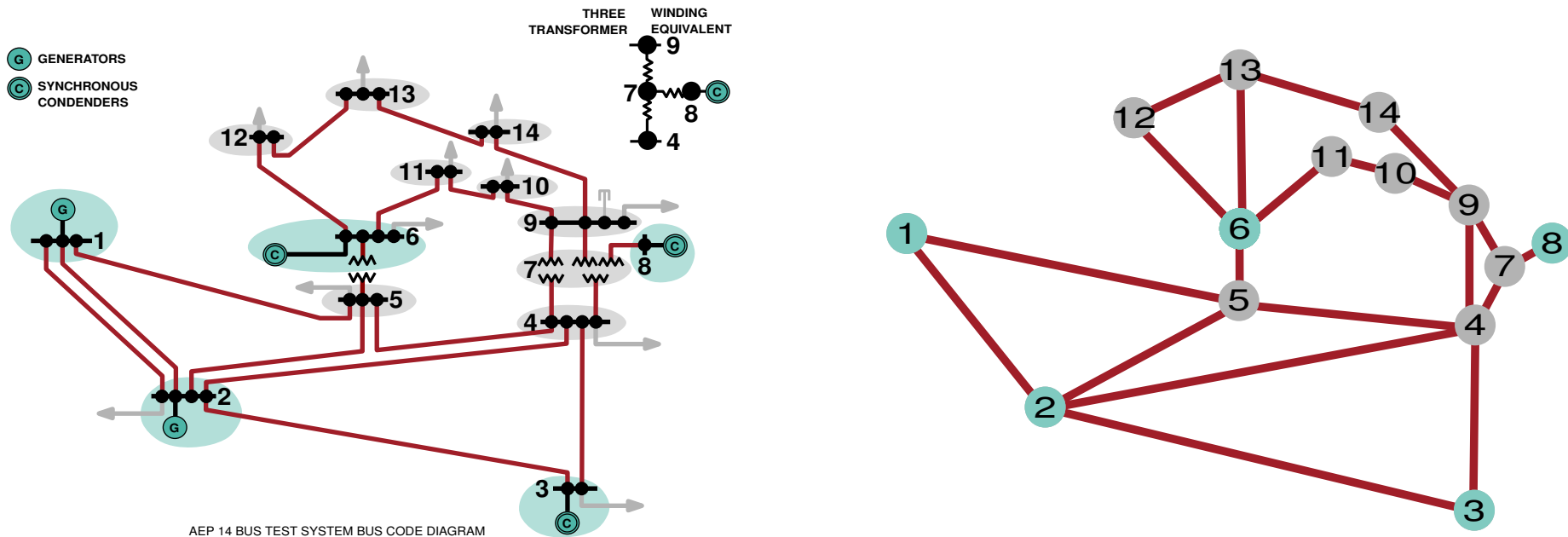
Straight-forward transformation:

- Power grid \rightarrow graph $G = (V, E)$
- Buses \rightarrow vertex set V
- **Branches** \rightarrow edge set E with capacity function $c(e)$



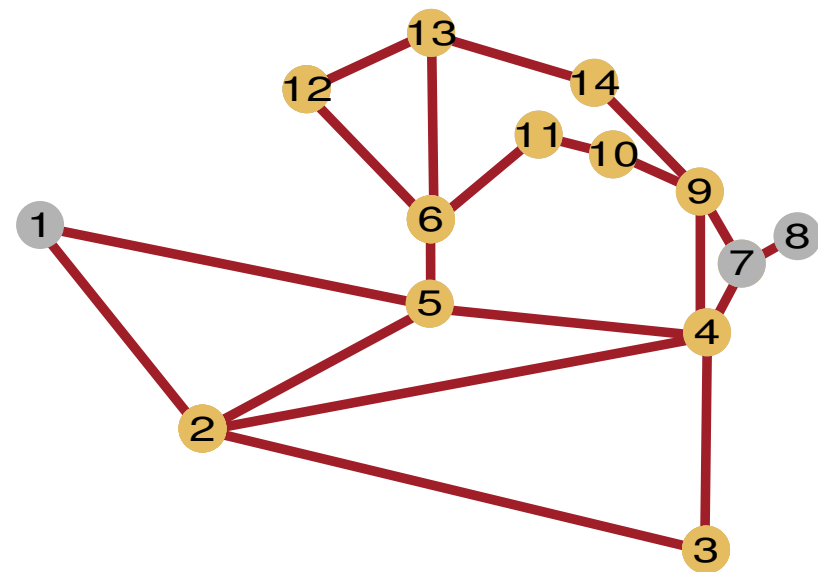
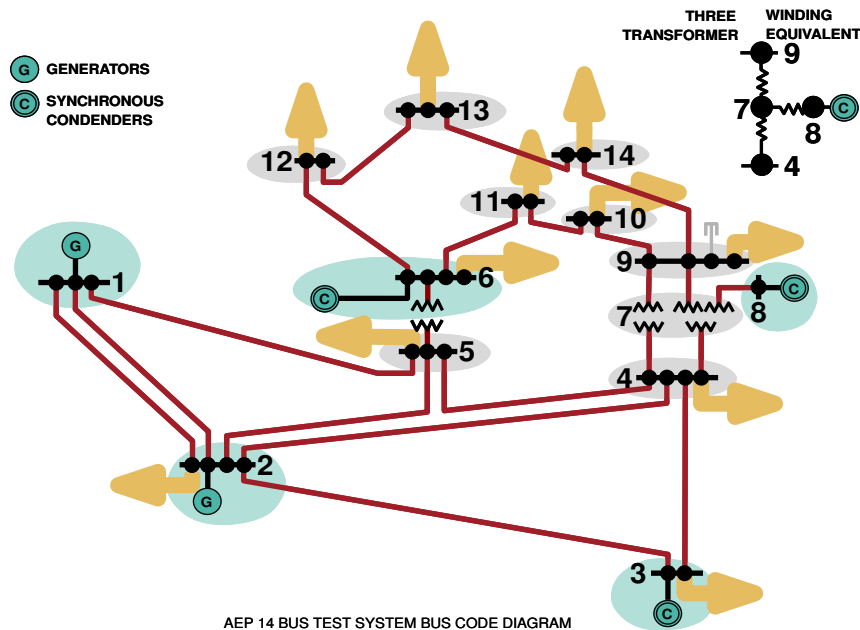
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- **Generators** \rightarrow set $V_G \subseteq V$ of generator buses

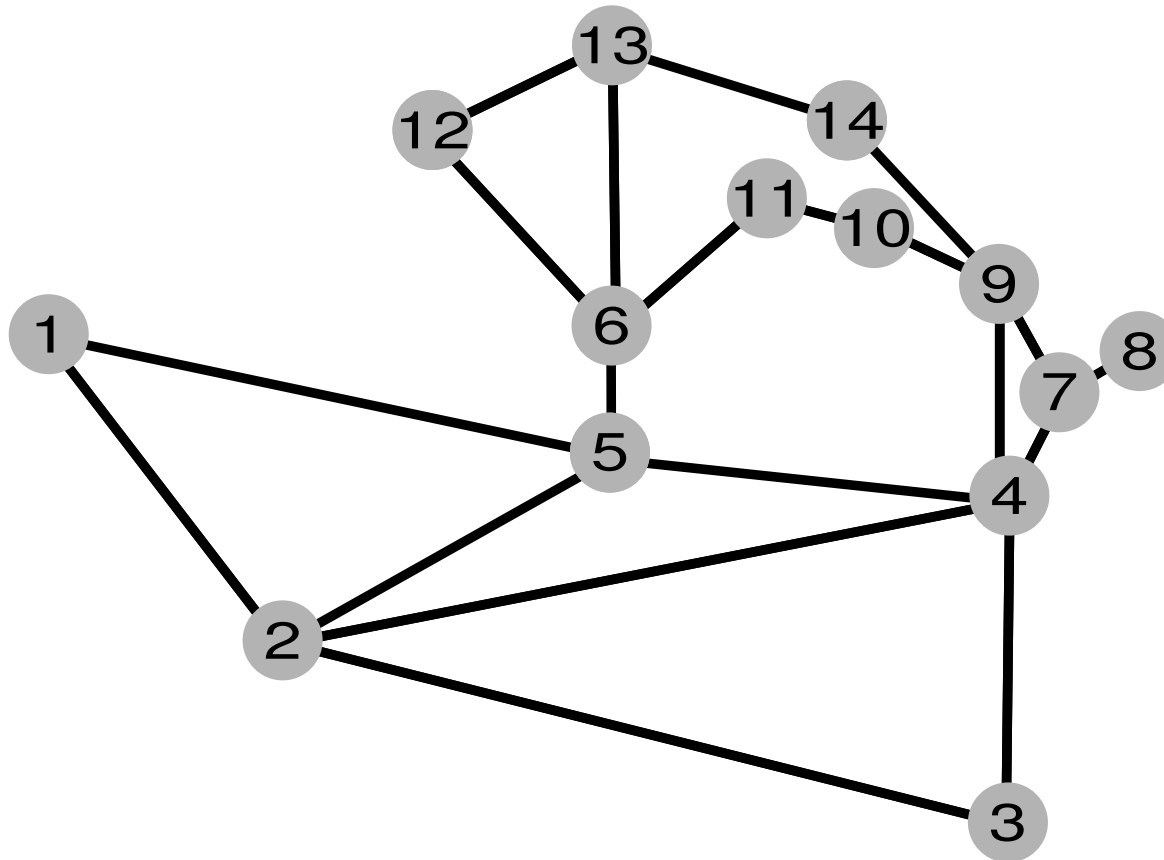


Straight-forward transformation:

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- Buses \rightarrow vertex set V
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- Generators \rightarrow set $V_G \subseteq V$ of generator buses
- Load \rightarrow set $V_L \subseteq V$ of load buses



Hybrid Flow Model



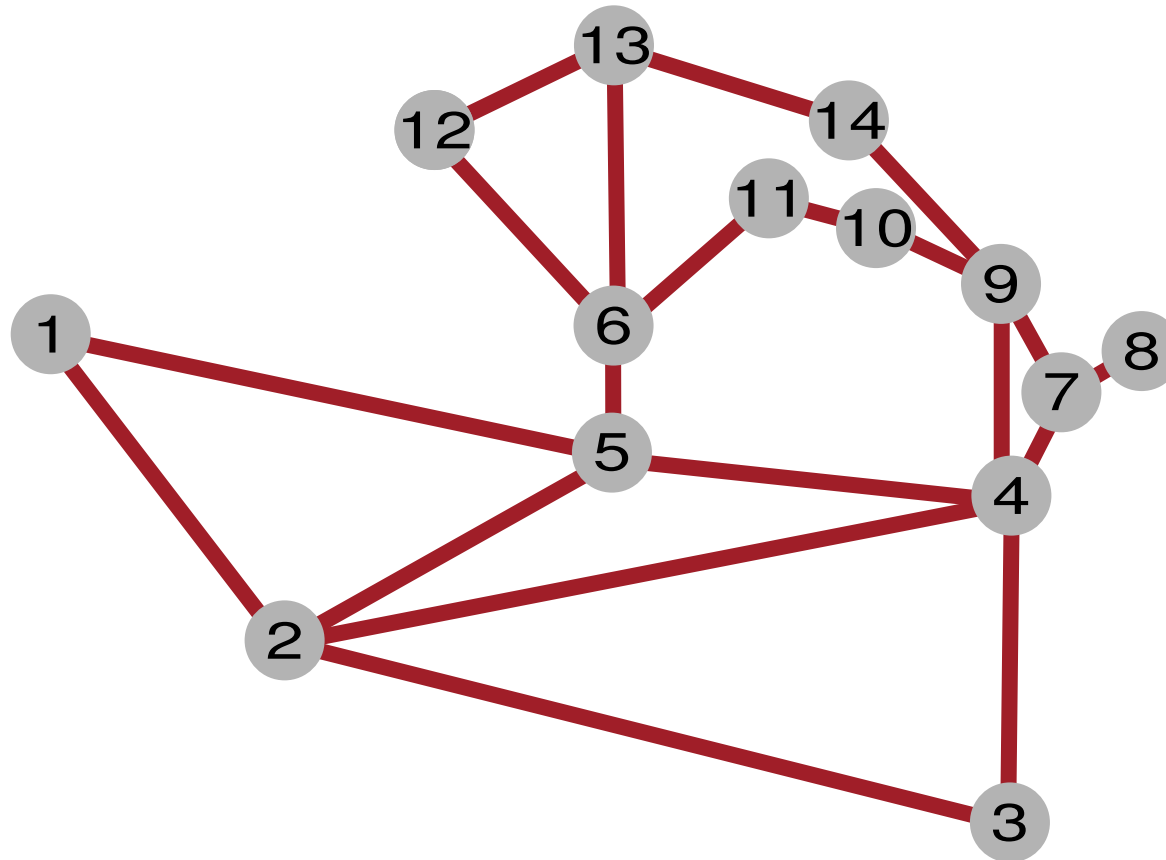
Kirchhoff's circuit laws:

Kirchhoff's current law ✓

Kirchhoff's voltage law ✓

Physical Model
(as a DC approximation)

Hybrid Flow Model



— control unit

Kirchhoff's circuit laws:

Kirchhoff's current law

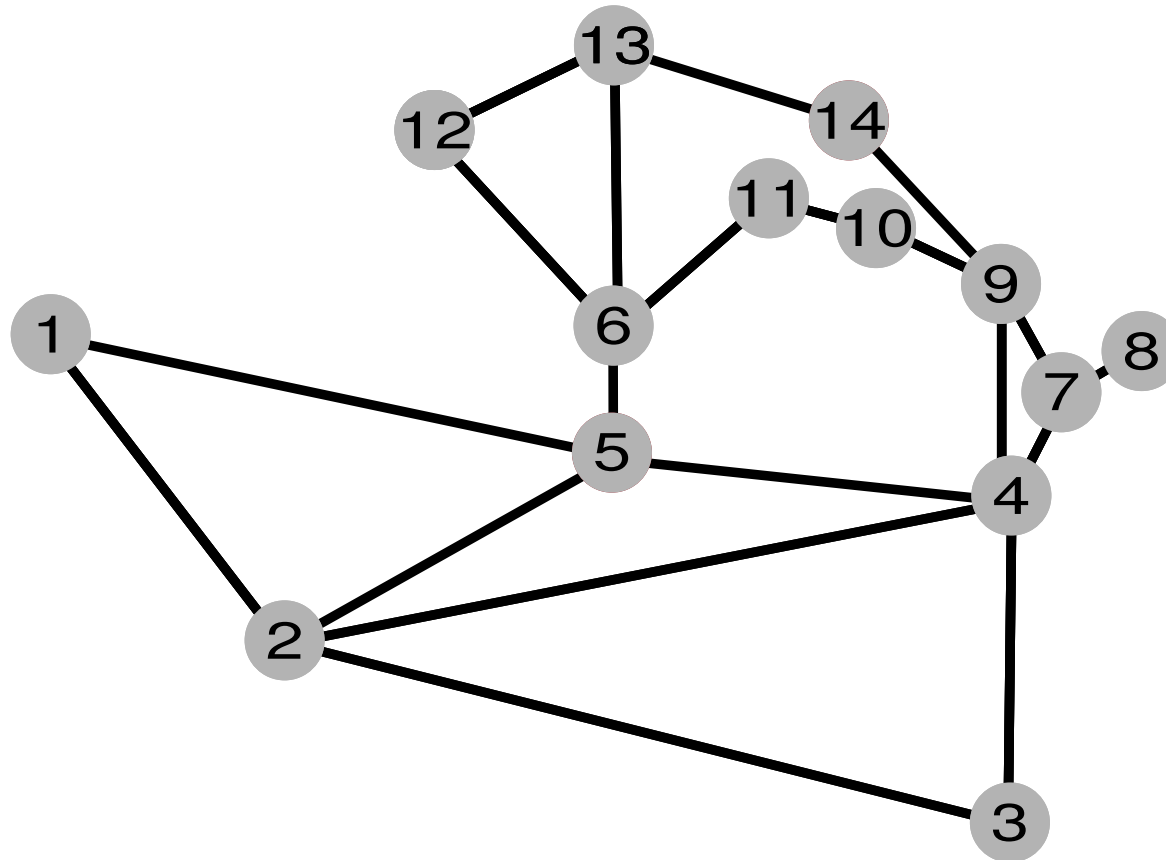
Kirchhoff's voltage law

Kirchhoff's current law ✓

Kirchhoff's voltage law ✗

Flow Model

Hybrid Flow Model



— control unit

Kirchhoff's circuit laws:

Kirchhoff's current law ✓

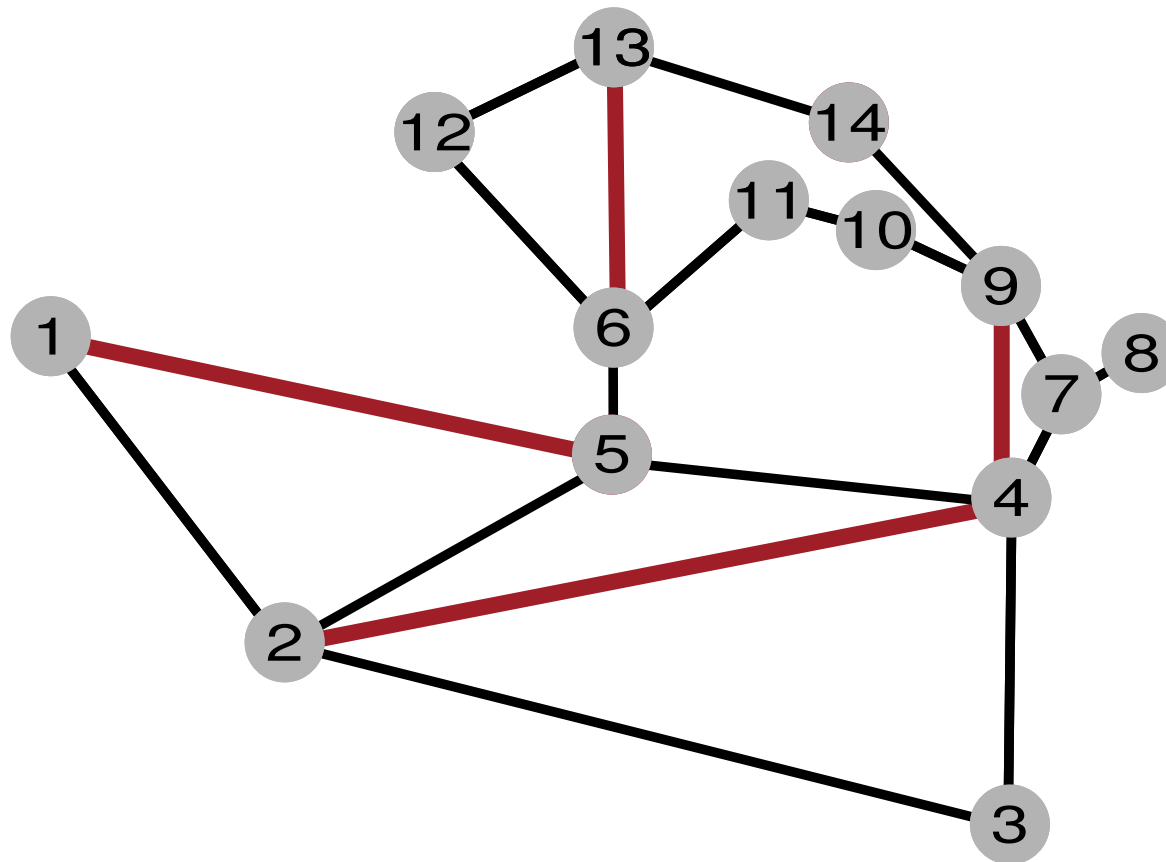
Kirchhoff's voltage law ✓

Kirchhoff's current law

Kirchhoff's voltage law

Hybrid Model = **Flow Model** + Physical Model

Hybrid Flow Model



— control unit

Kirchhoff's circuit laws:

Kirchhoff's current law ✓

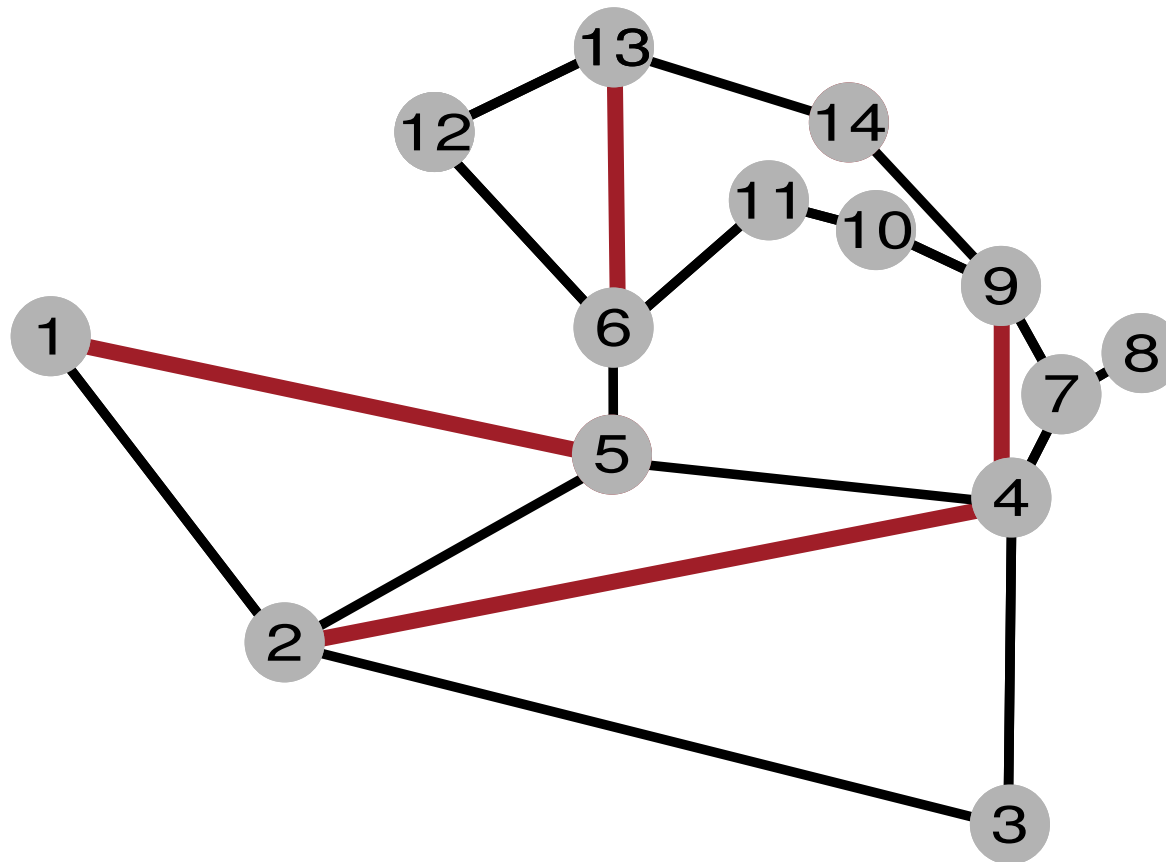
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Hybrid Model = Flow Model + Physical Model

Hybrid Flow Model



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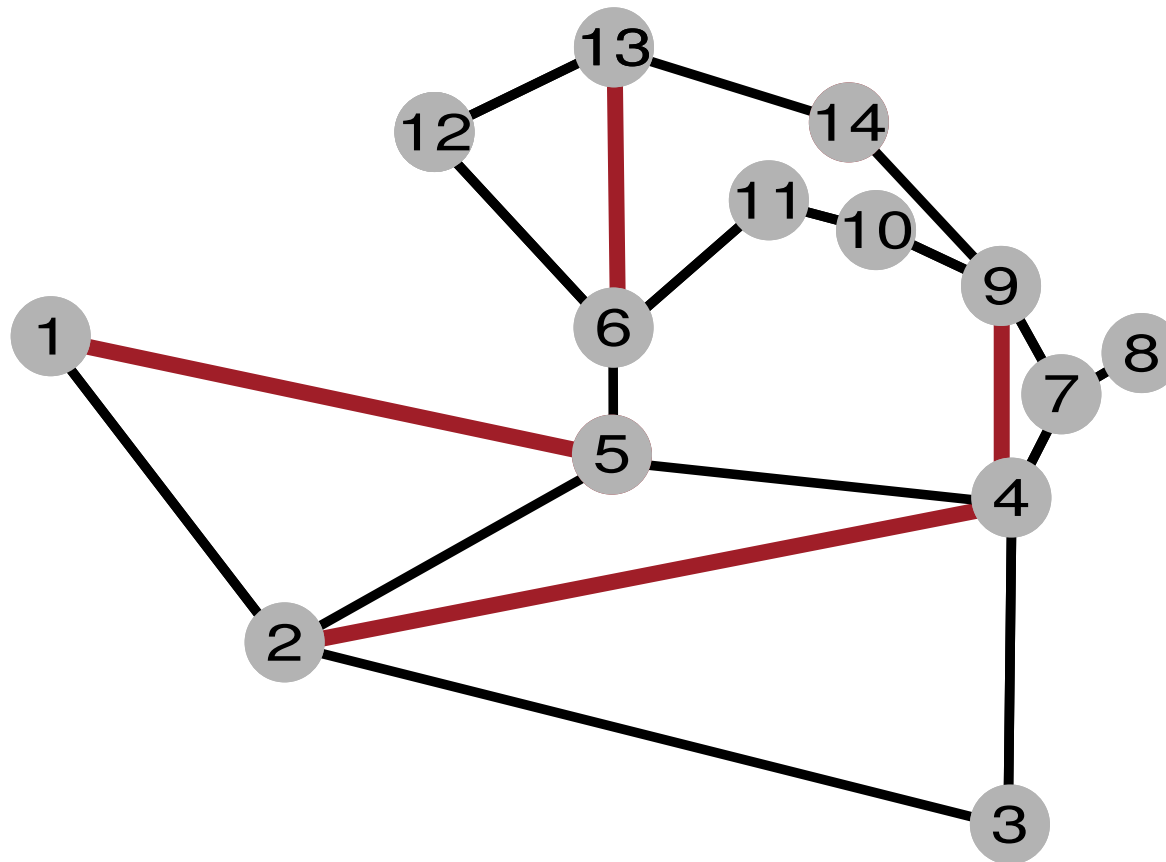
Kirchhoff's current law ✓

Kirchhoff's voltage law ✗

Hybrid Model = Flow Model + Physical Model

⇓
Lower Bound

Hybrid Flow Model



— control unit

Kirchhoff's circuit laws:

Kirchhoff's current law ✓

Kirchhoff's voltage law ✓

Kirchhoff's current law ✓

Kirchhoff's voltage law ✗

Hybrid Model = **Flow Model** + Physical Model

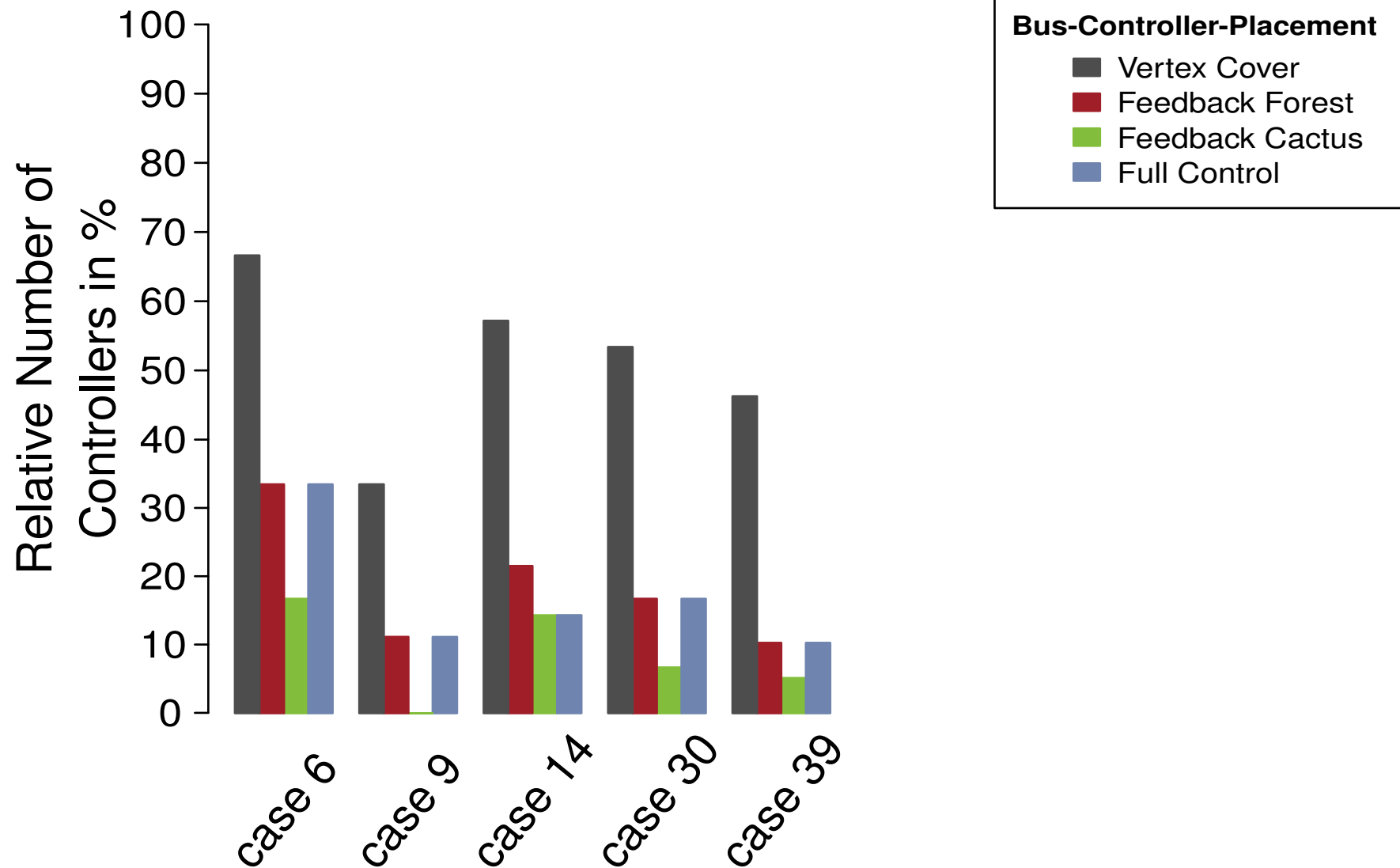
⇓
Lower Bound

⇓
Upper Bound

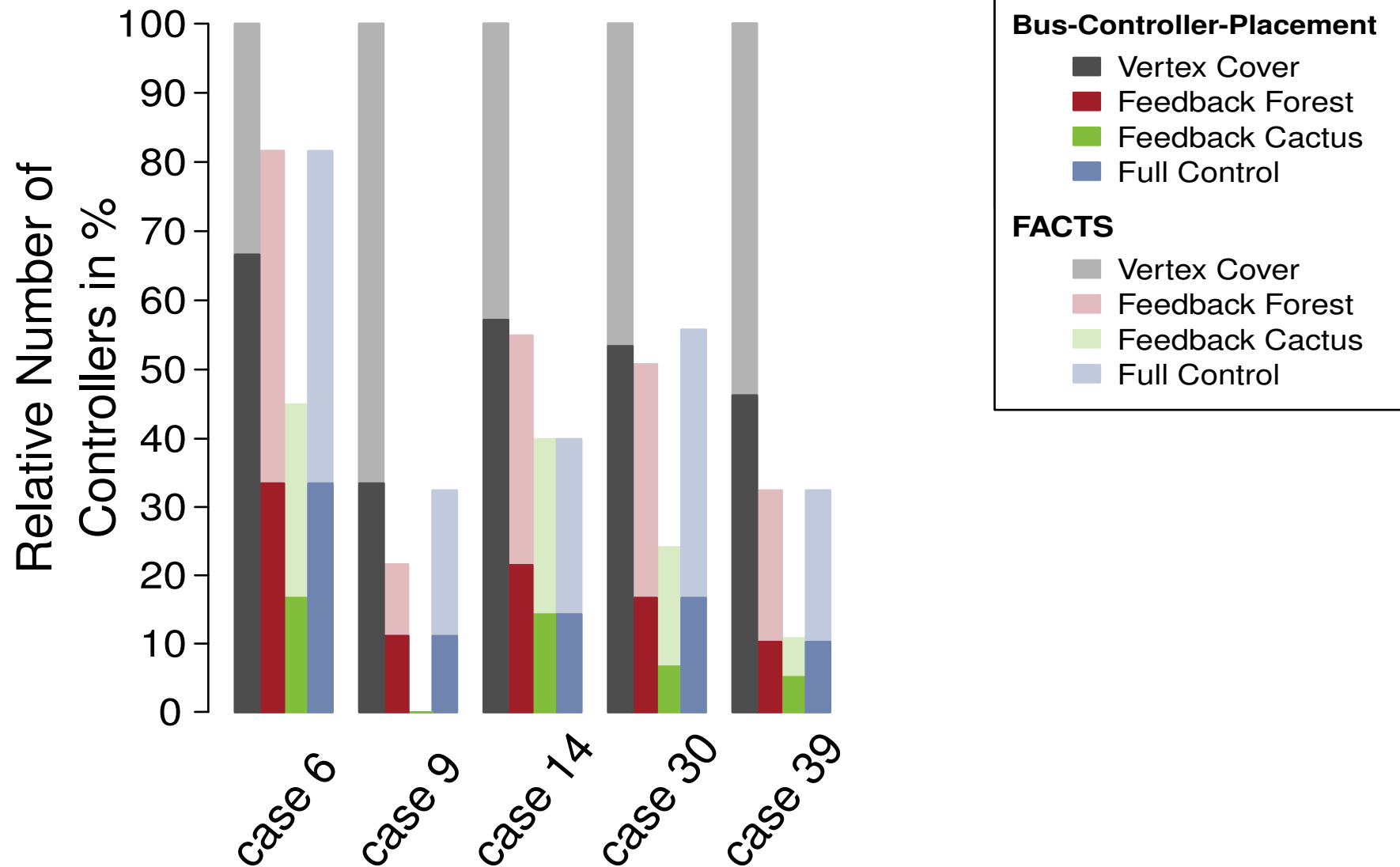
Control units are expensive – how many do we need?

- (Q1) How many controlled branches are necessary for globally optimal power flows? Which branches need to be controlled?
- (Q2) For a given number of available control branches, is there a positive effect on flow costs and operability when approaching grid capacity limits?

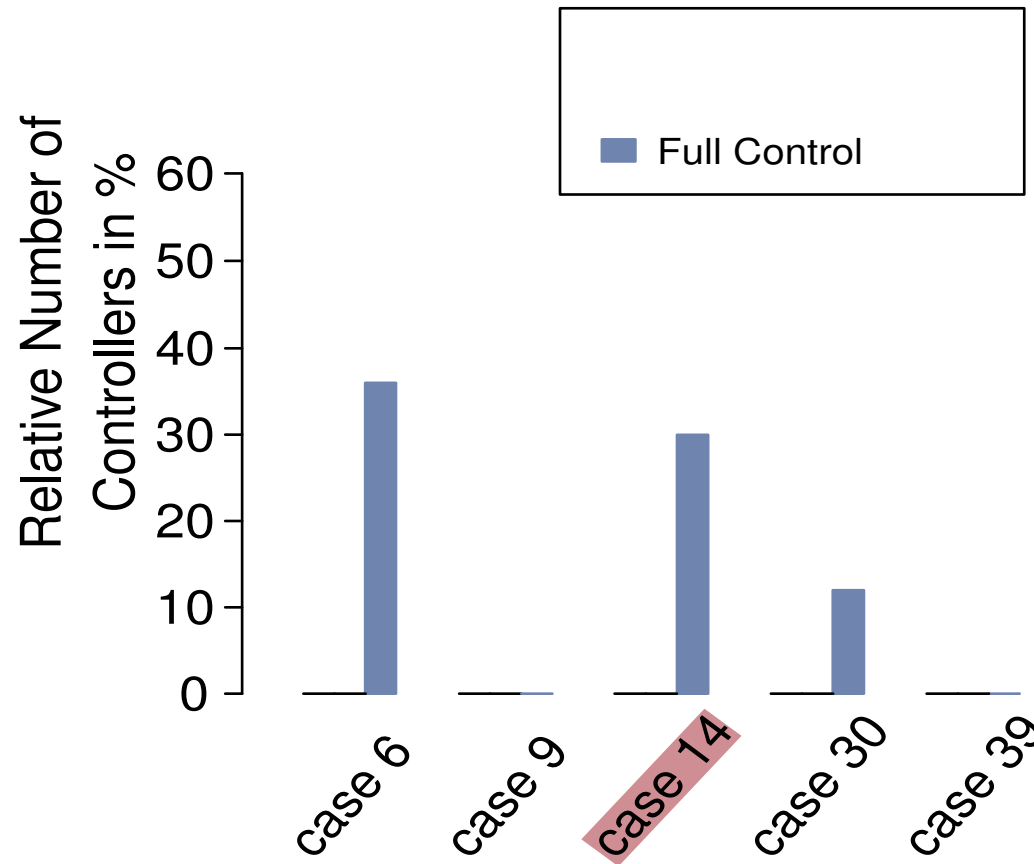
Controller Placement on Buses [Leibfried et al., 2015]



Controller Placement on Buses [Leibfried et al., 2015]



Number of Control Branches



- For each benchmark case: $\max_{\lambda} \min \#Controller$

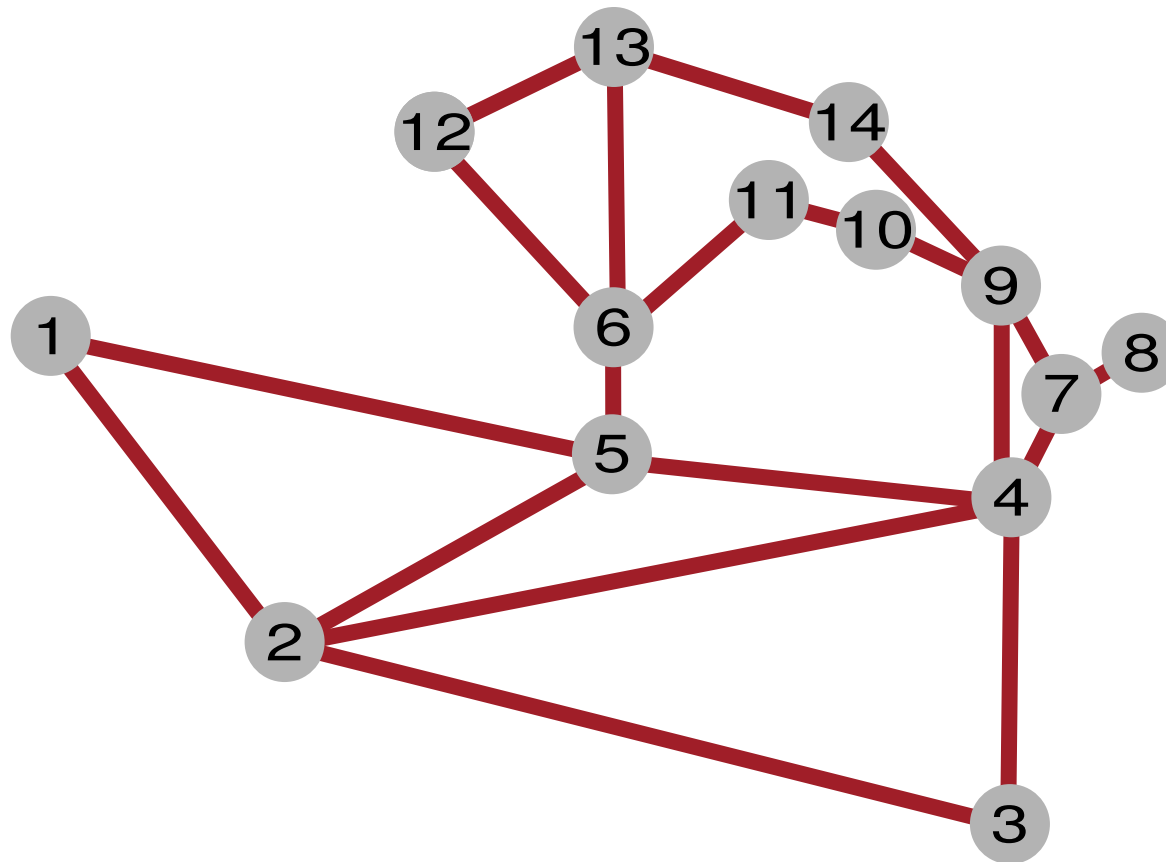


Matching the Flow Model (Q1)

- How many flow control branches are necessary to obtain globally optimal power flows and which branches need to be controlled?

Left Figure:
² http://www.lichtenwald-mentaltraining.de/files/bild.licht_im_wald.jpg

Globally Optimal Power Flows

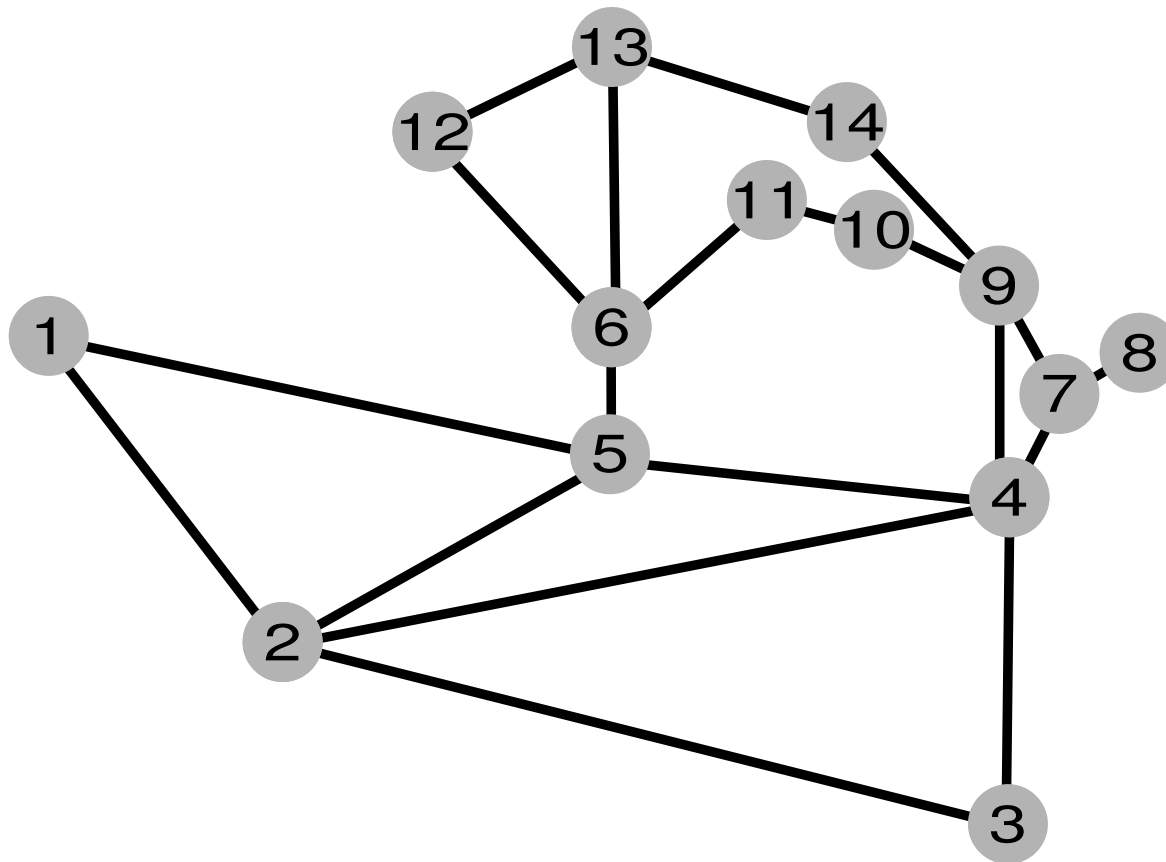


— control unit

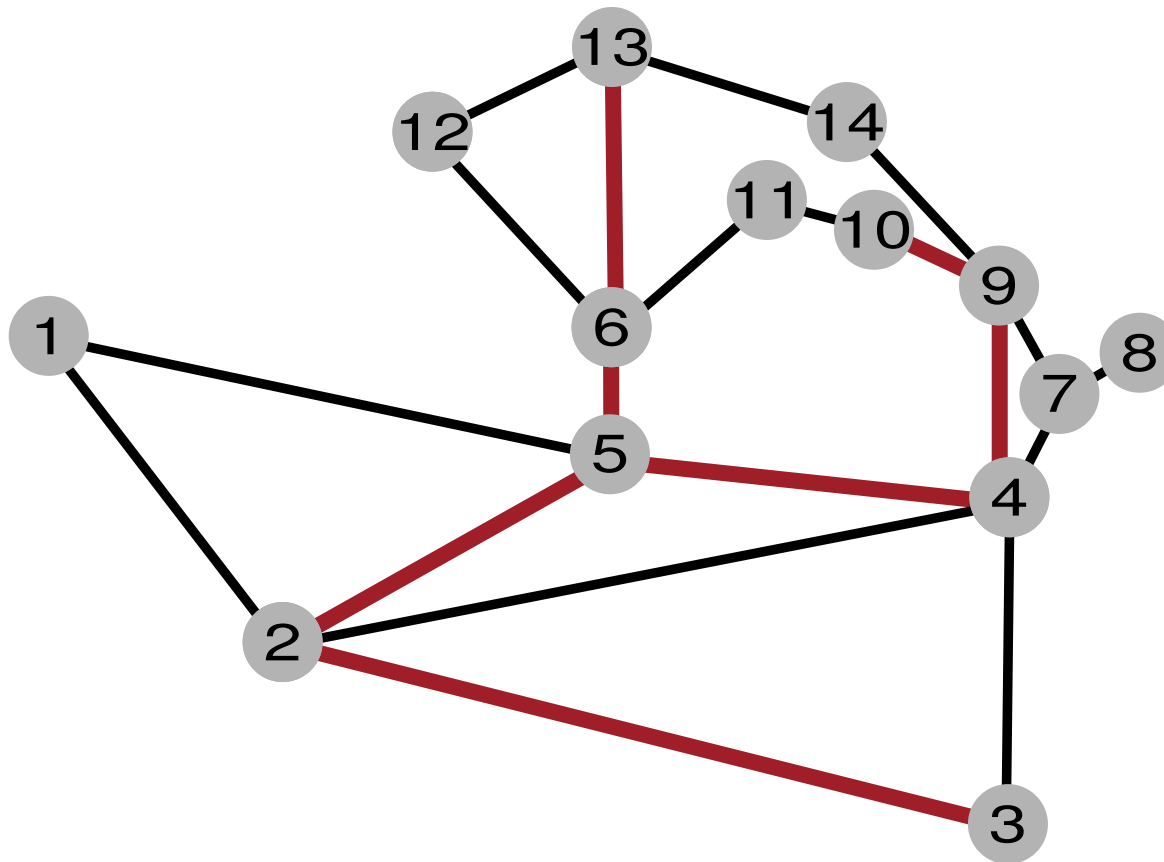
Can we become as good as the **Flow Model** with fewer control branches?

Feedback Forest Set

 *feedback forest set*



Feedback Forest Set

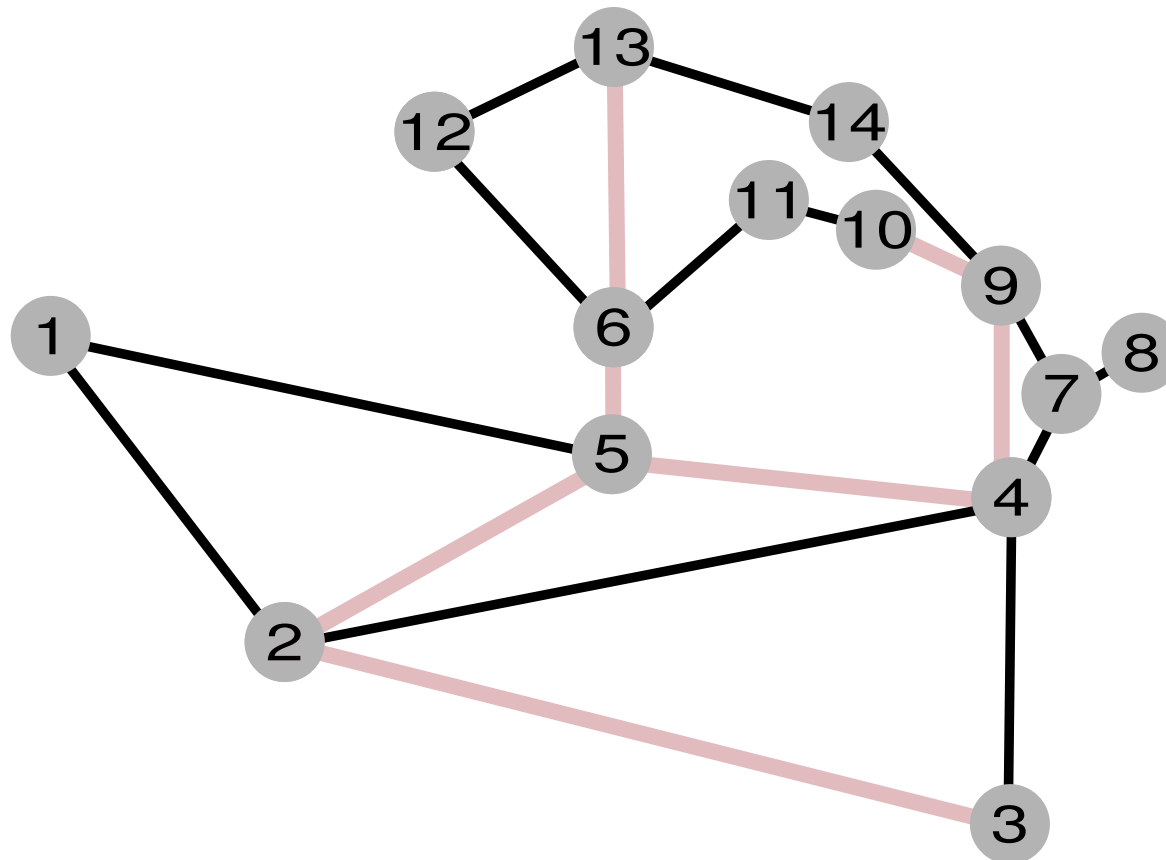


 *feedback forest set*



A set of trees (*forest*)
remains!

Feedback Forest Set



 *feedback forest set*



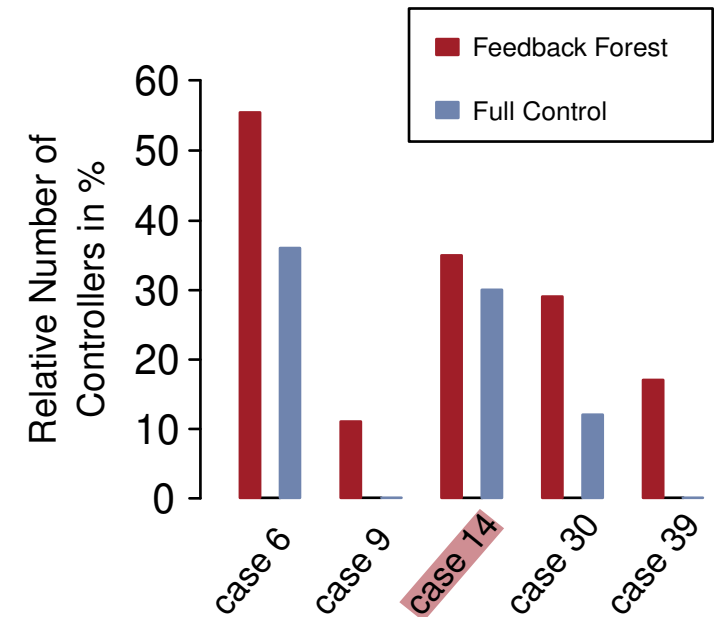
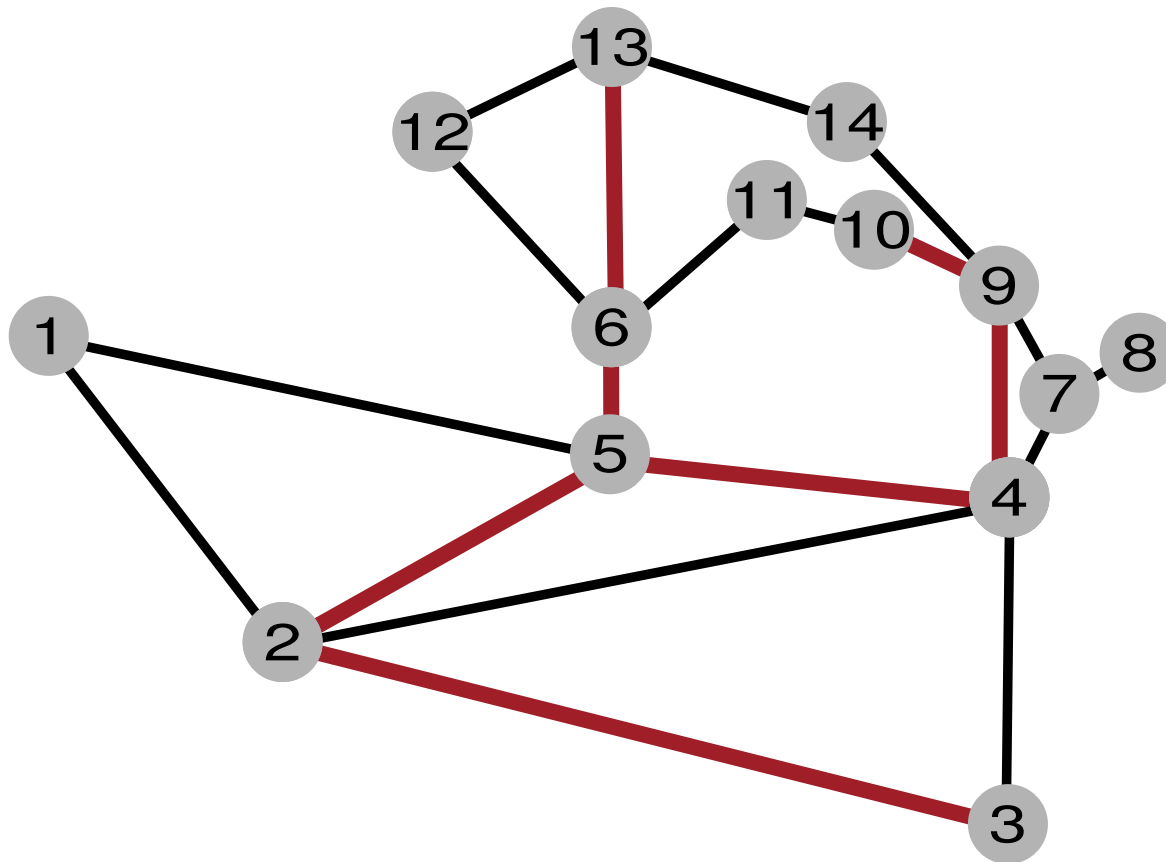
A set of trees (*forest*)
remains!

Theorem 1

Physical subgrid forest \Rightarrow All flows obey voltage laws

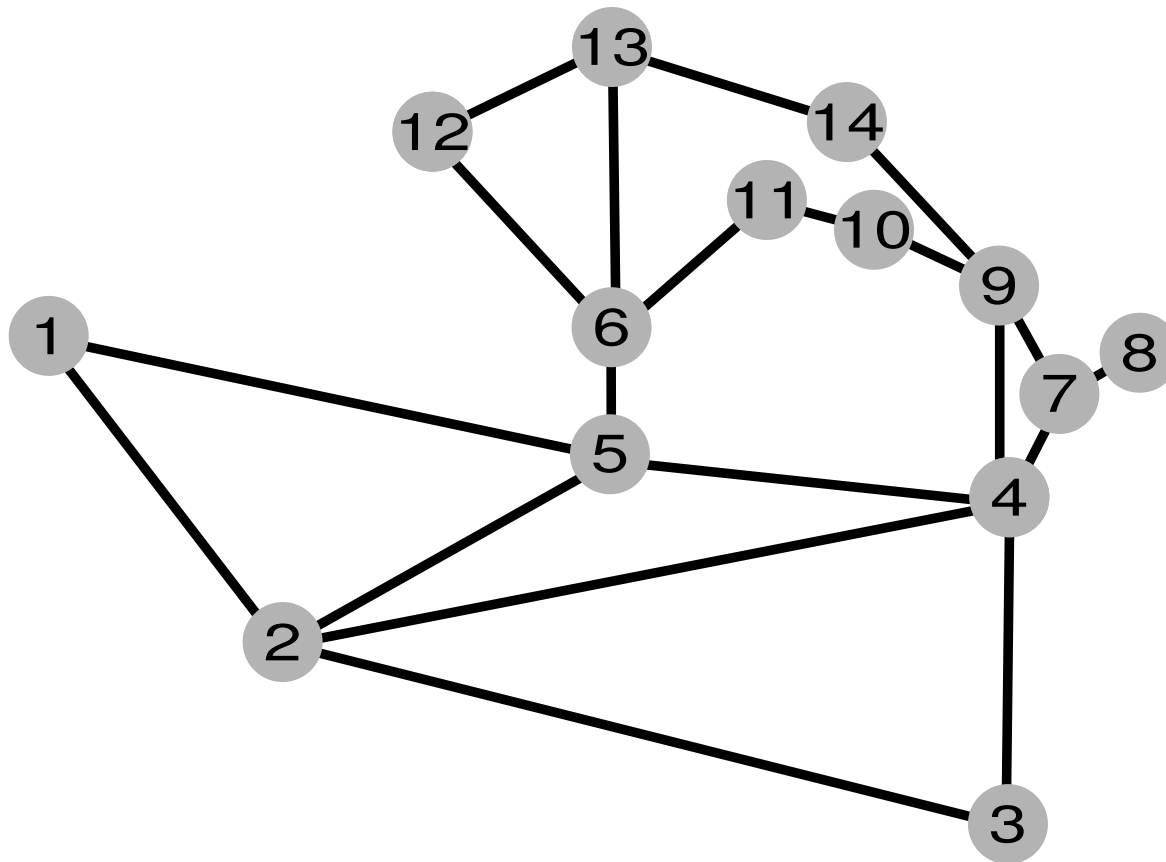
Feedback Cactus Set

 *feedback forest set*



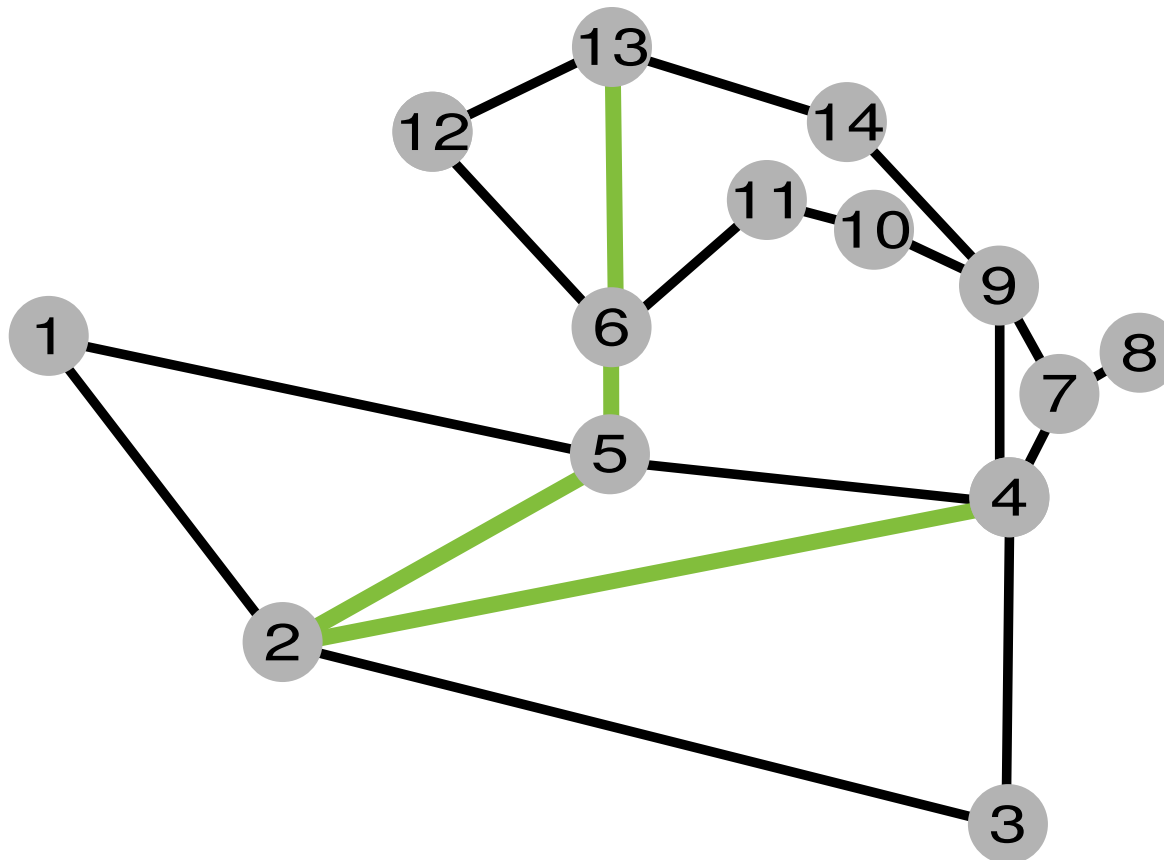
Fewer than **7** flow control buses sufficient?

Feedback Cactus Set



 *feedback cactus set*

Feedback Cactus Set

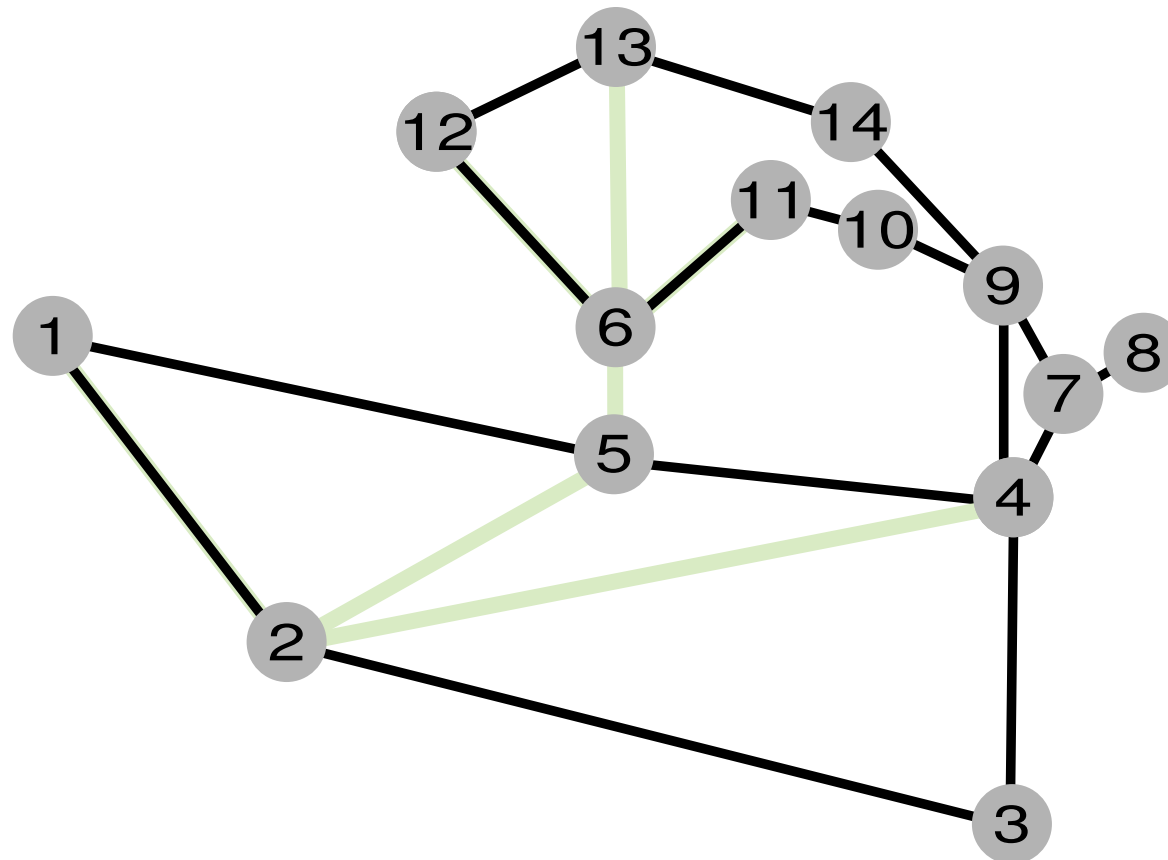



 *feedback cactus set*



A set of *cacti* remains!

Feedback Cactus Set



 *feedback cactus set*
↓
A set of *cacti* remains!

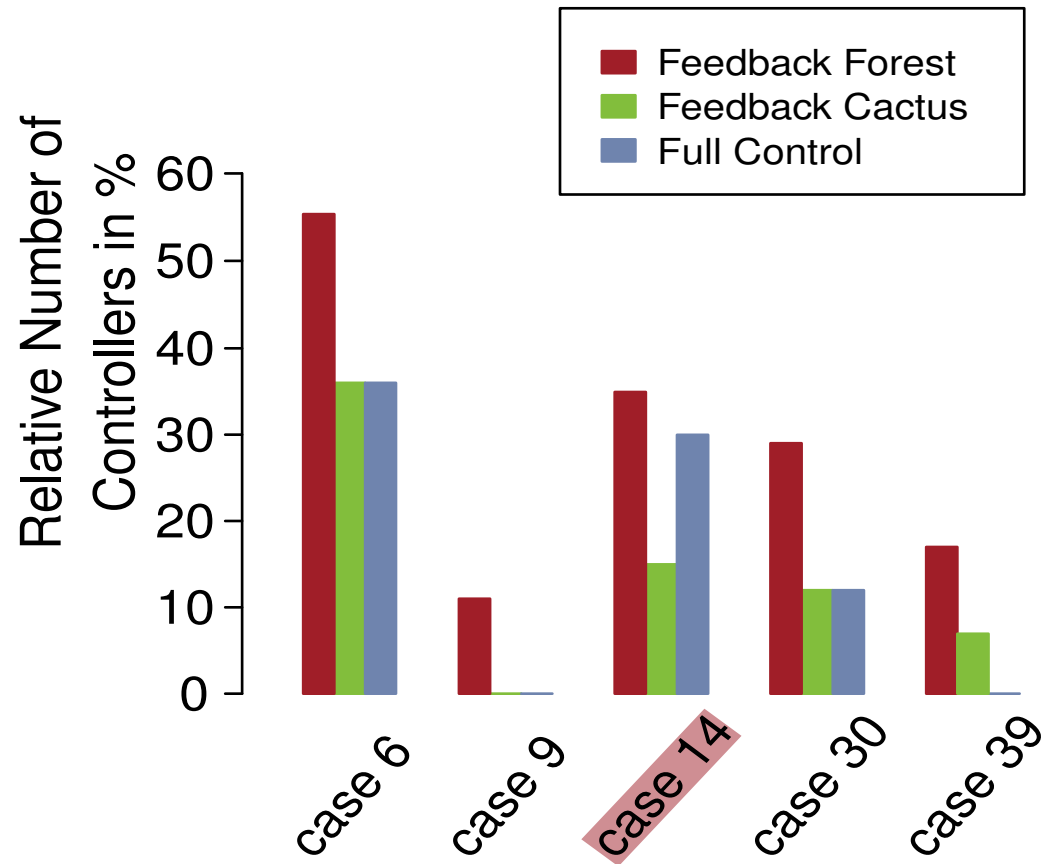
Theorem 2

Physical subgrid cactus, line limits on cactus suitably bounded.

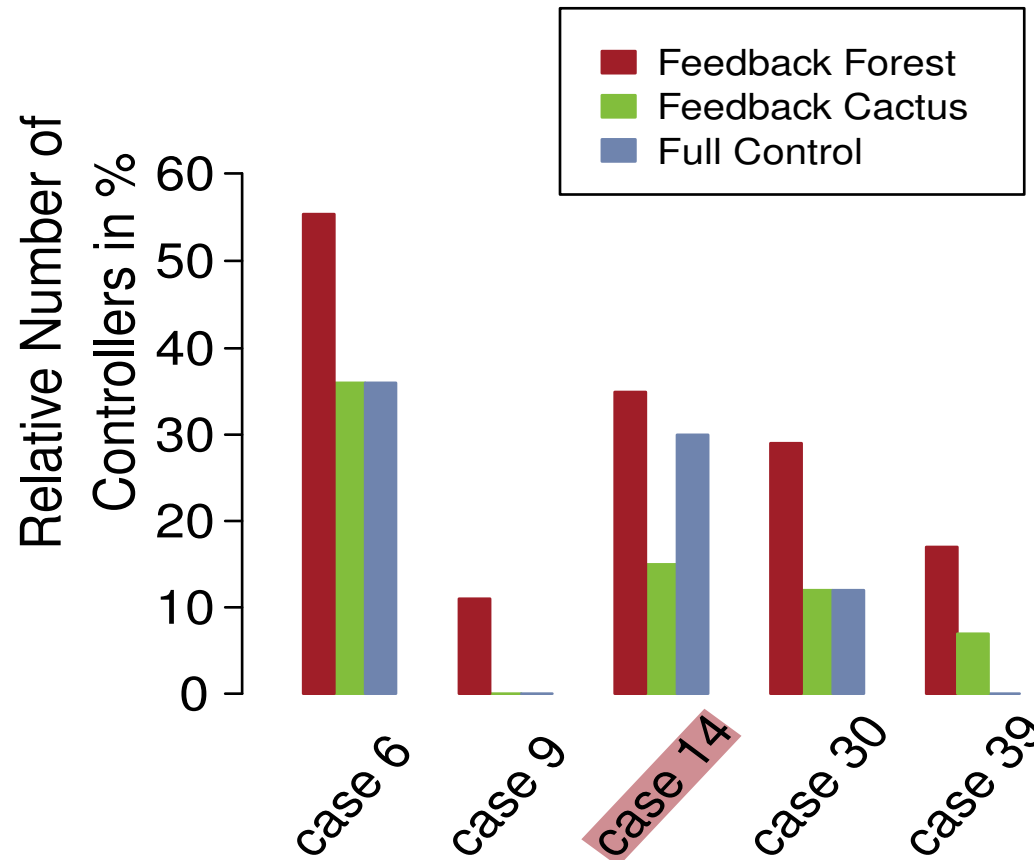
⇒

For every flow there is a cost-equivalent flow obeying voltage laws.

Number of Control Branches vs. Structural Results



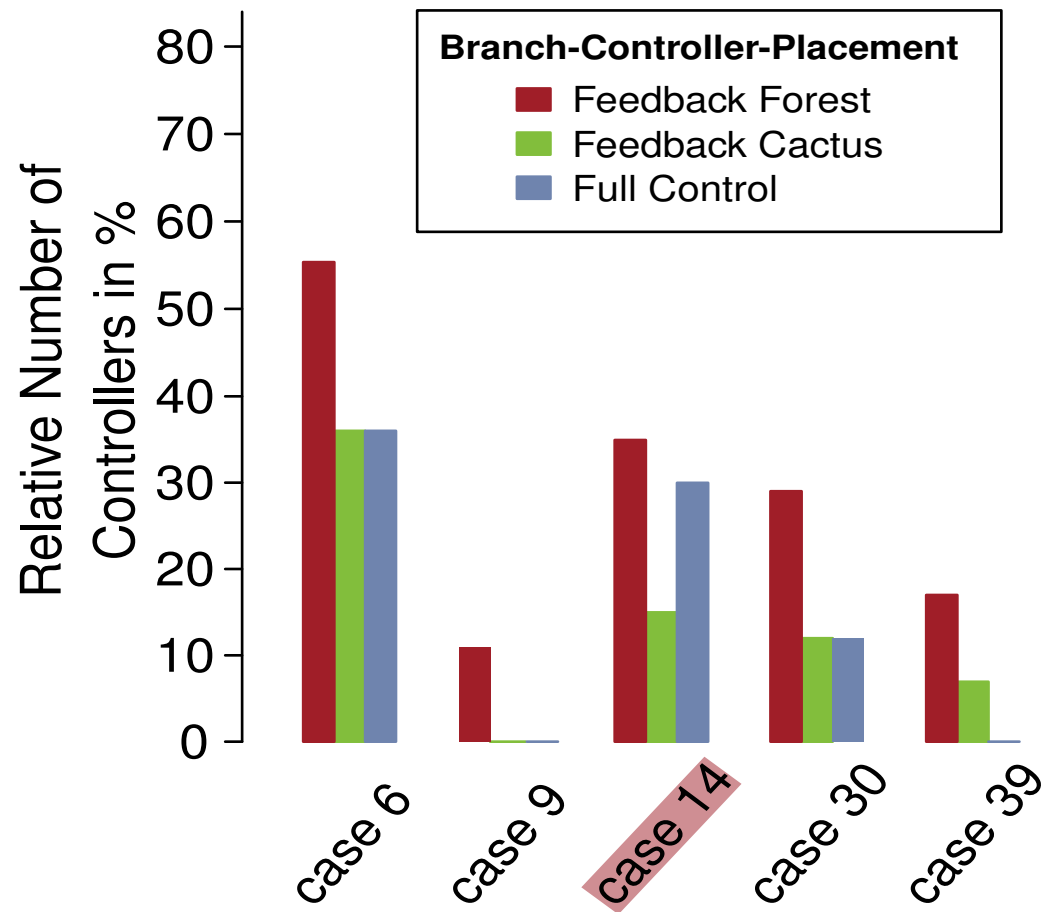
Number of Control Branches vs. Structural Results



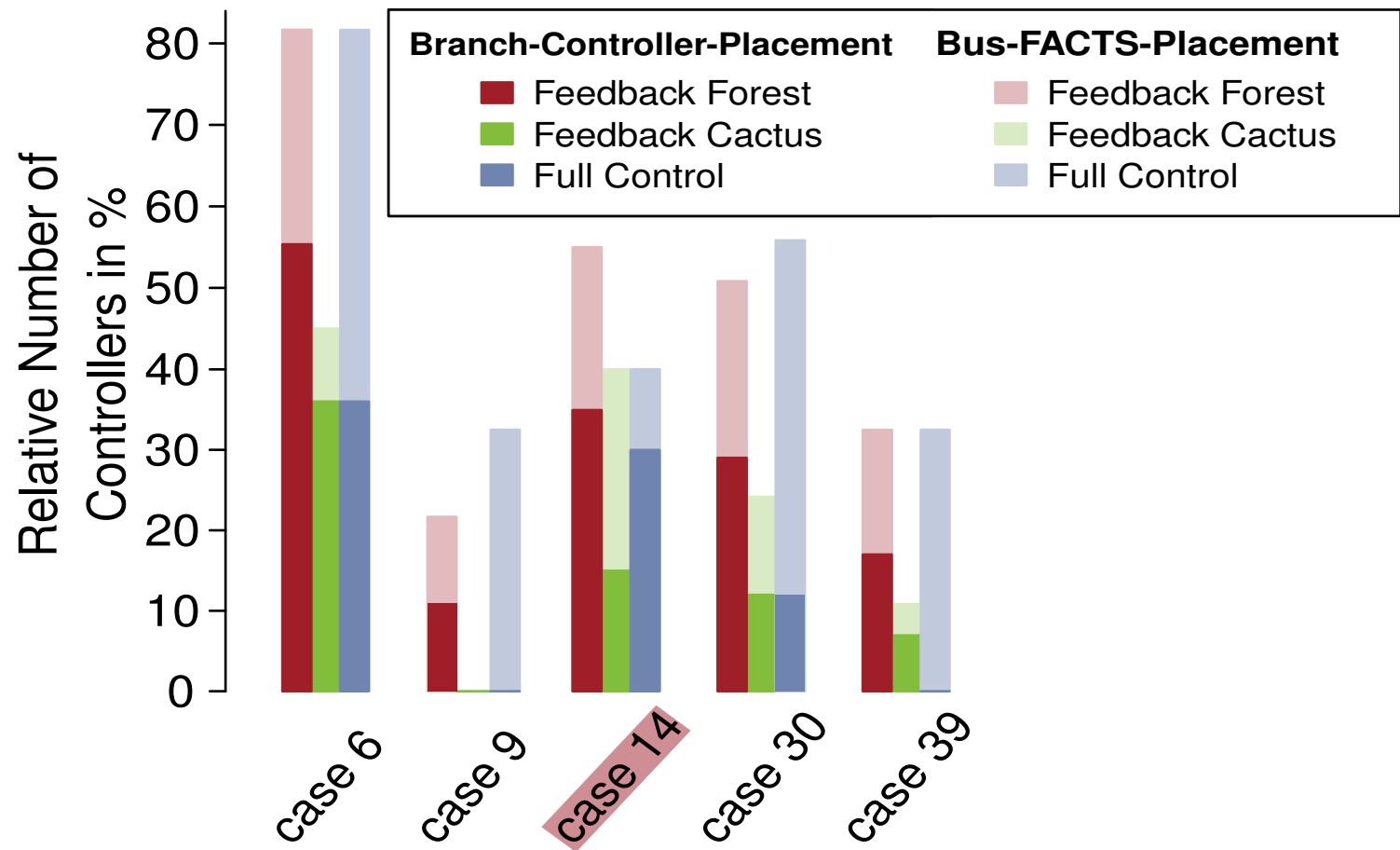
Findings

Often a small number of flow control branches suffices for matching cost of the flow model.

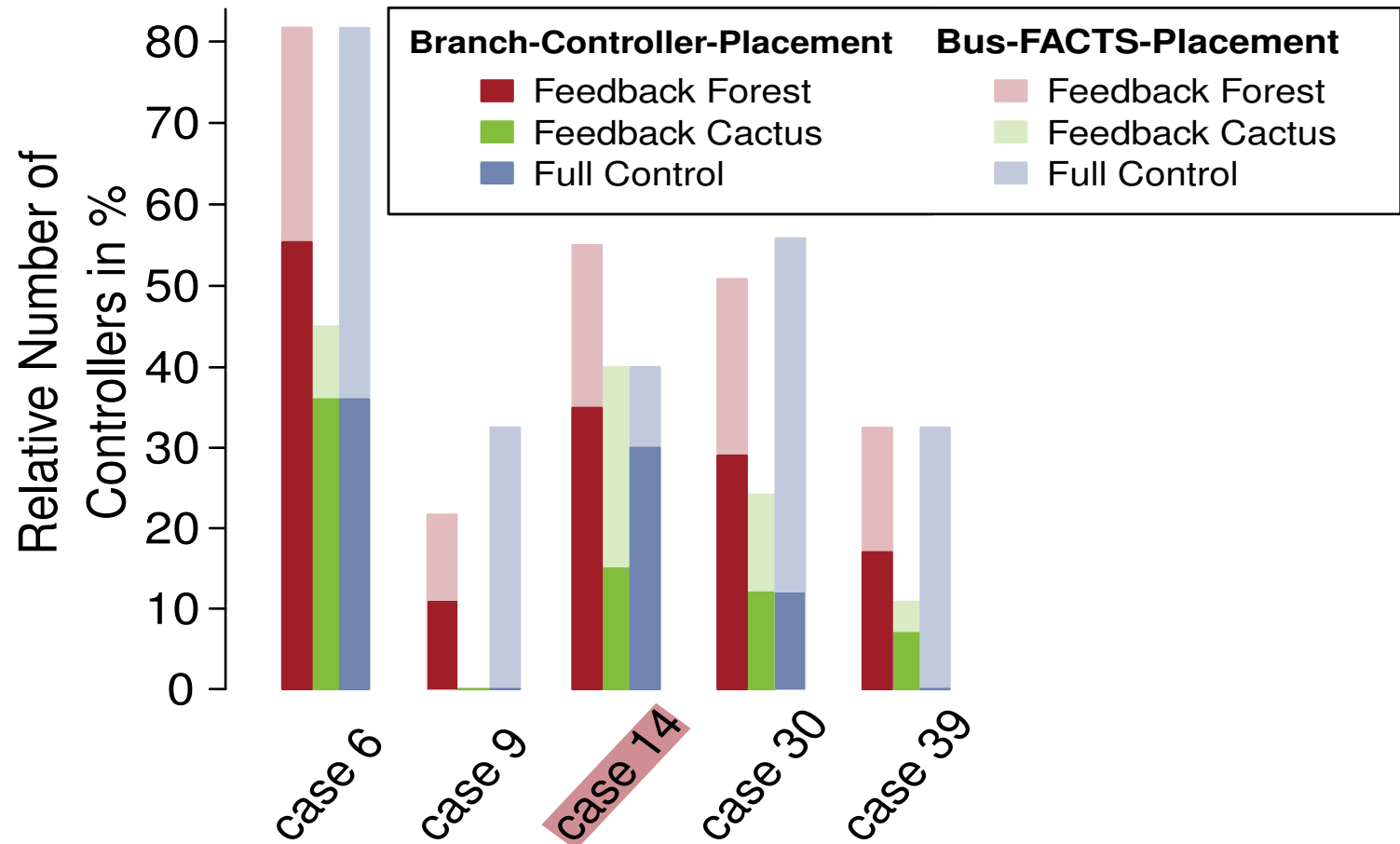
Control Branches vs. Control Buses



Control Branches vs. Control Buses



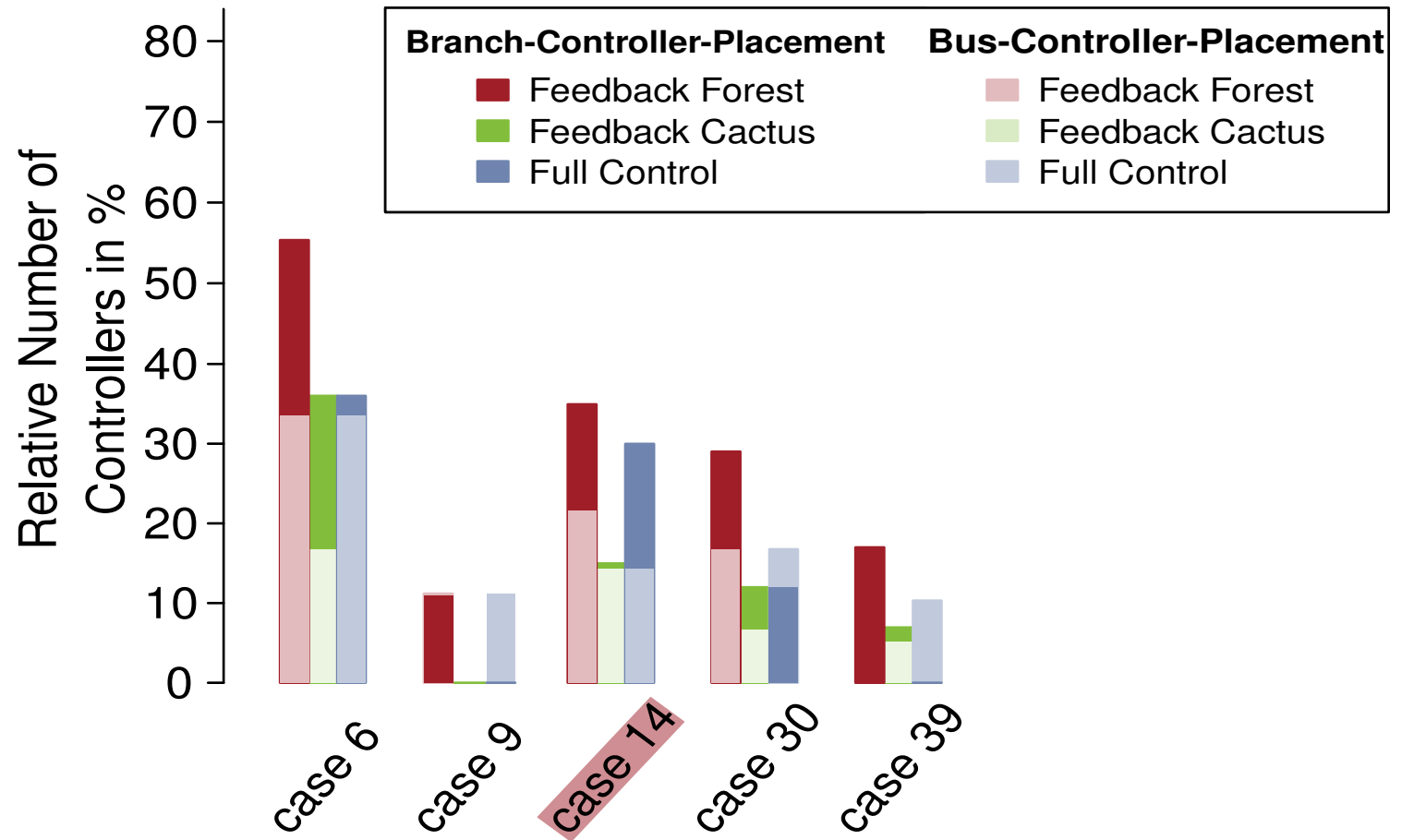
Control Branches vs. Control Buses



Findings

Smaller number of FACTS are sufficient for placing controller on branches rather than buses.

Control Branches vs. Control Buses





Effect of Few Flow Control Branches (Q2)

- For a given number of available control branches, is there a positive effect on flow costs and operability when approaching grid capacity limits?

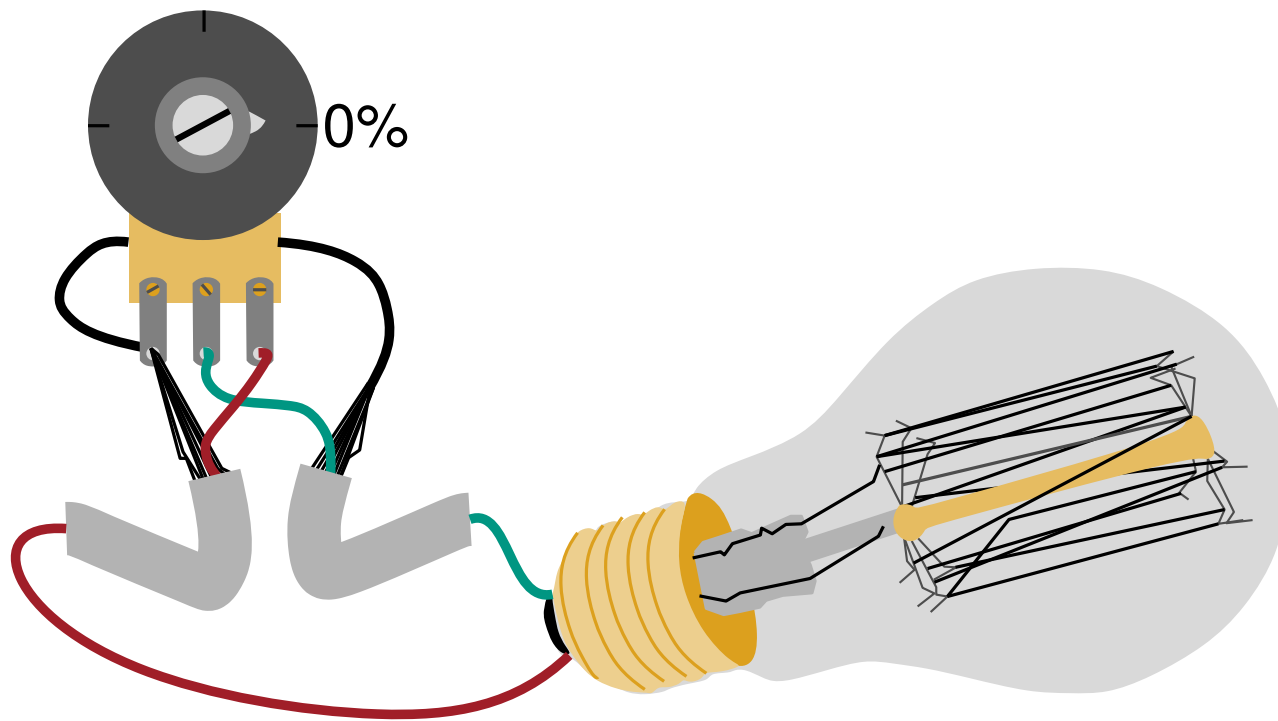
Figures FLTR:

³ <http://www.abb.com/cawp/seitp202/c36f4e62da52ab46c1257670003690d3.aspx>

⁴ <http://electrical-engineering-portal.com/facts-flexible-ac-transmission-systems>

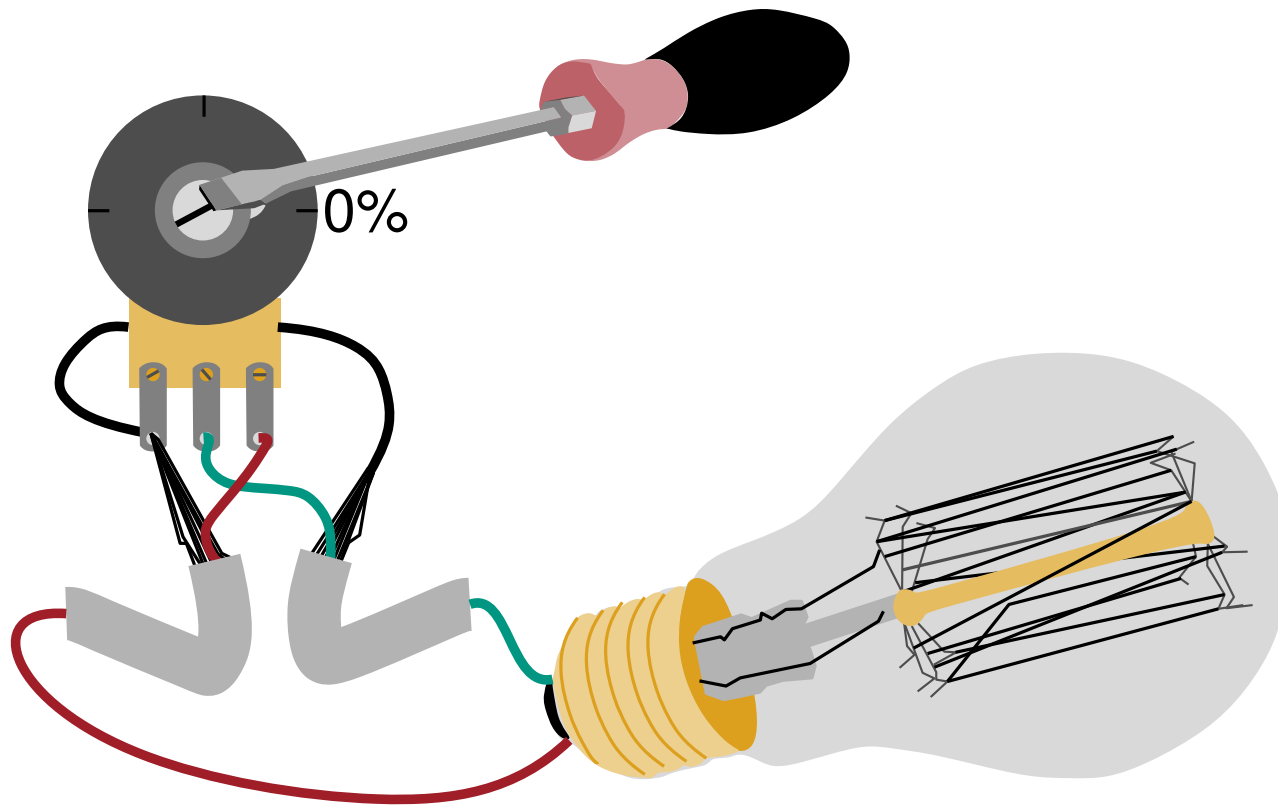
Effect of Few Flow Control Branches

Simulate load increase by a load increase factor ρ ,



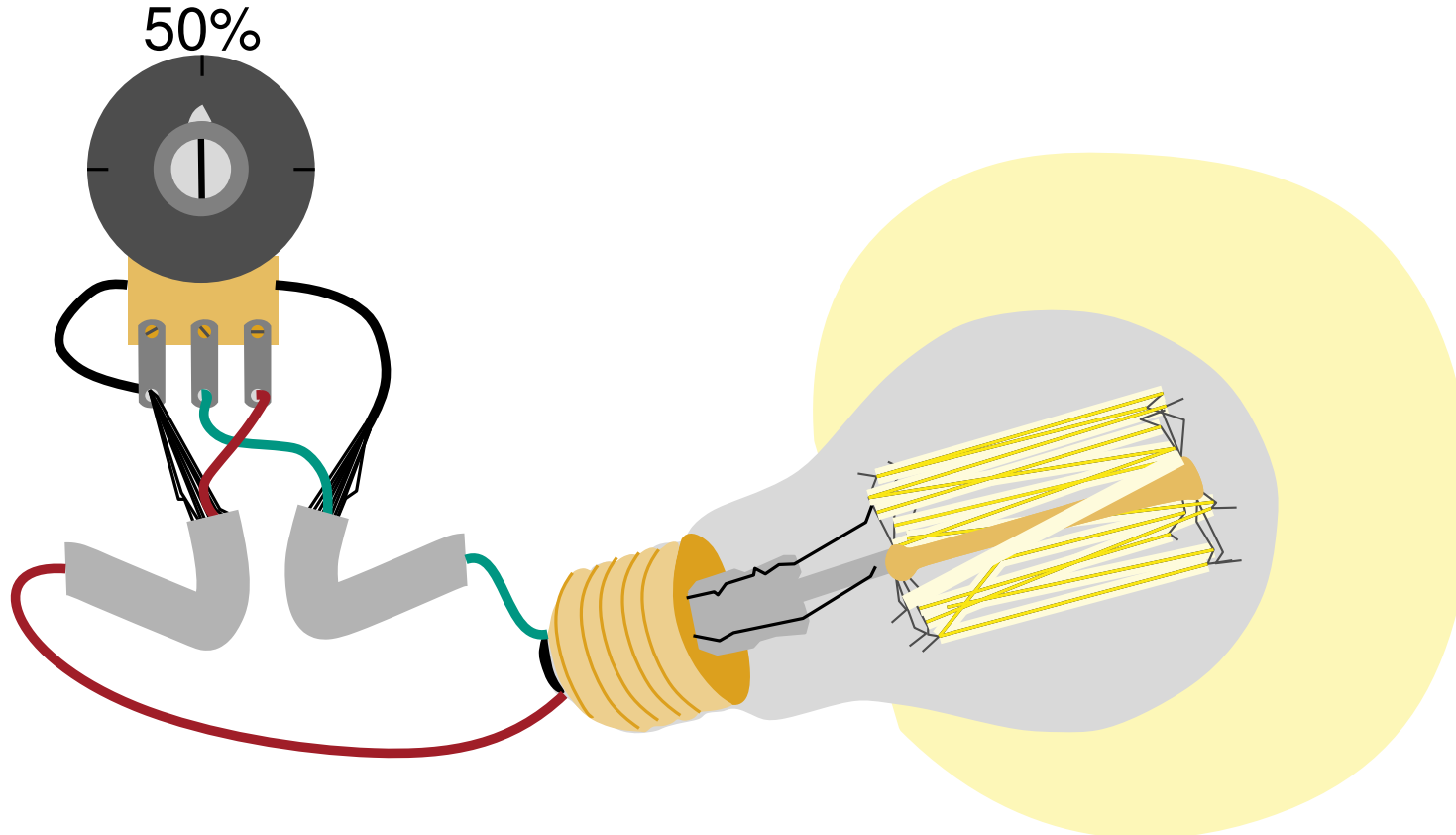
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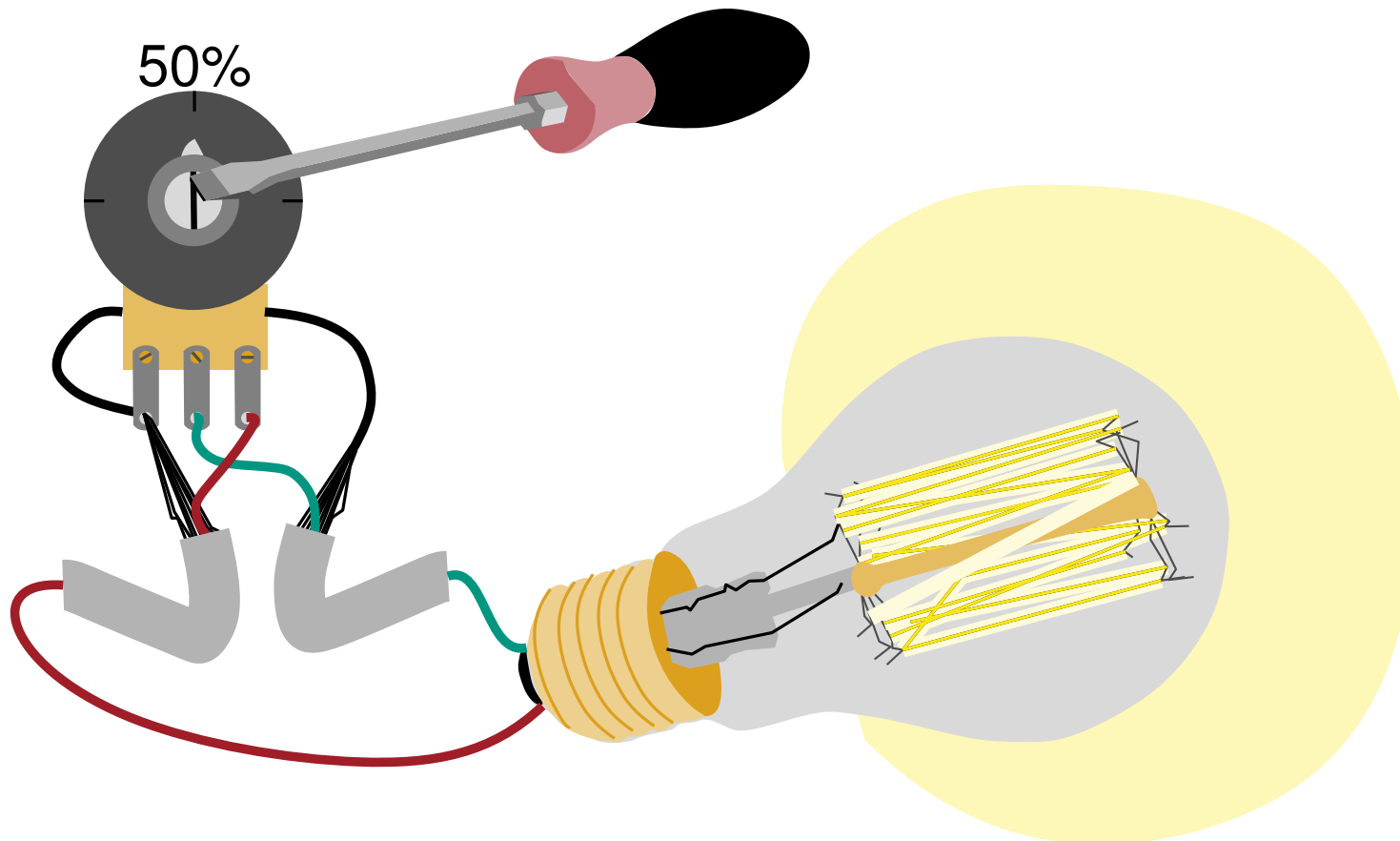
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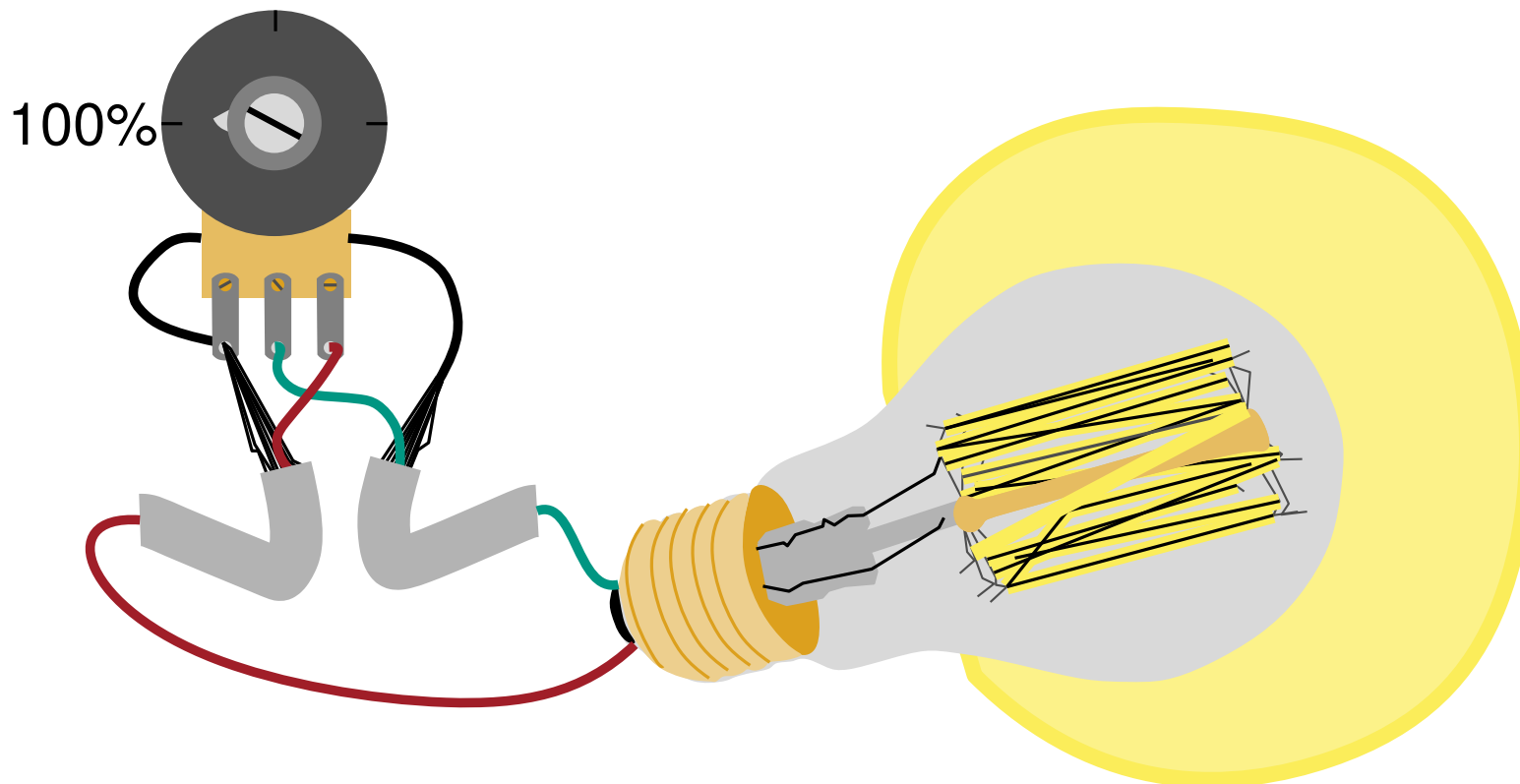
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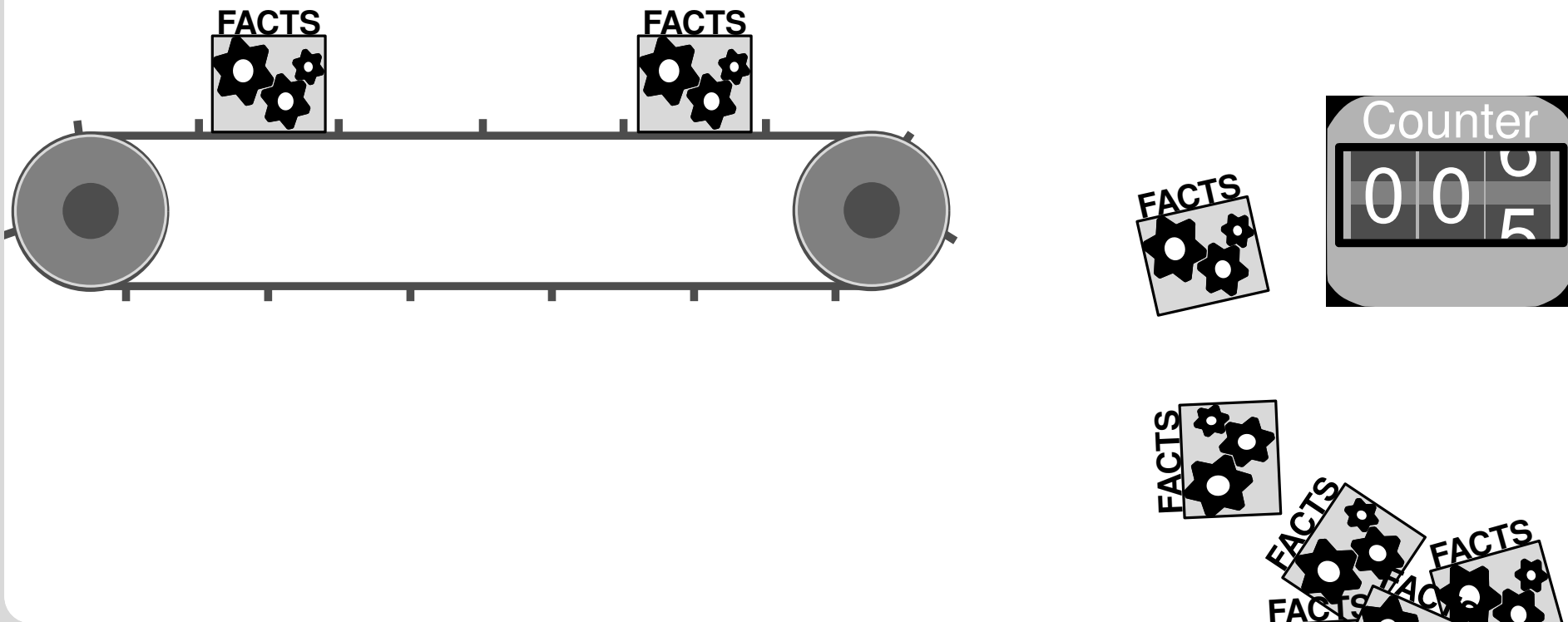
Effect of Few Flow Control Branches

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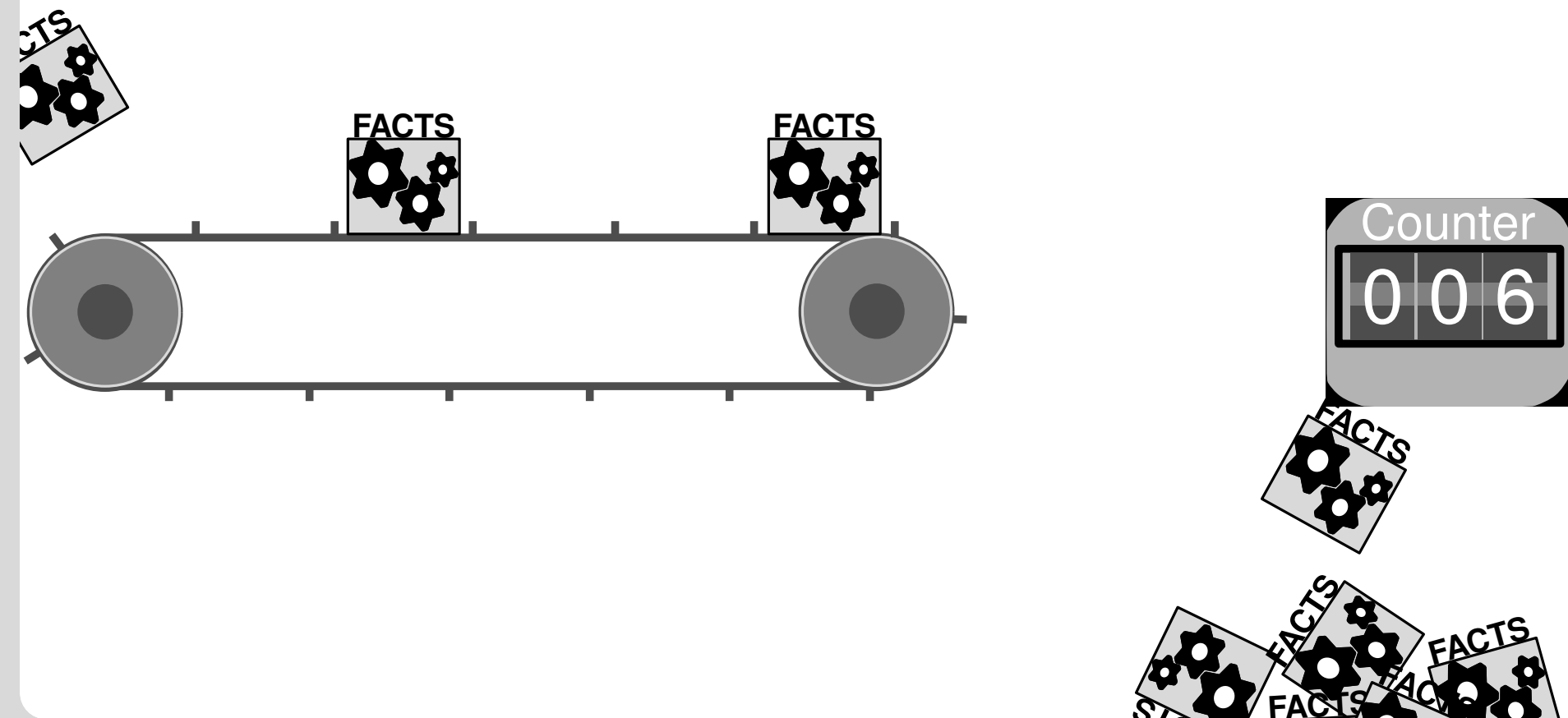
Effect of Few Flow Control Branches

Simulate load increase by a load increase factor ρ ,
Simulations with different numbers of flow controllers.



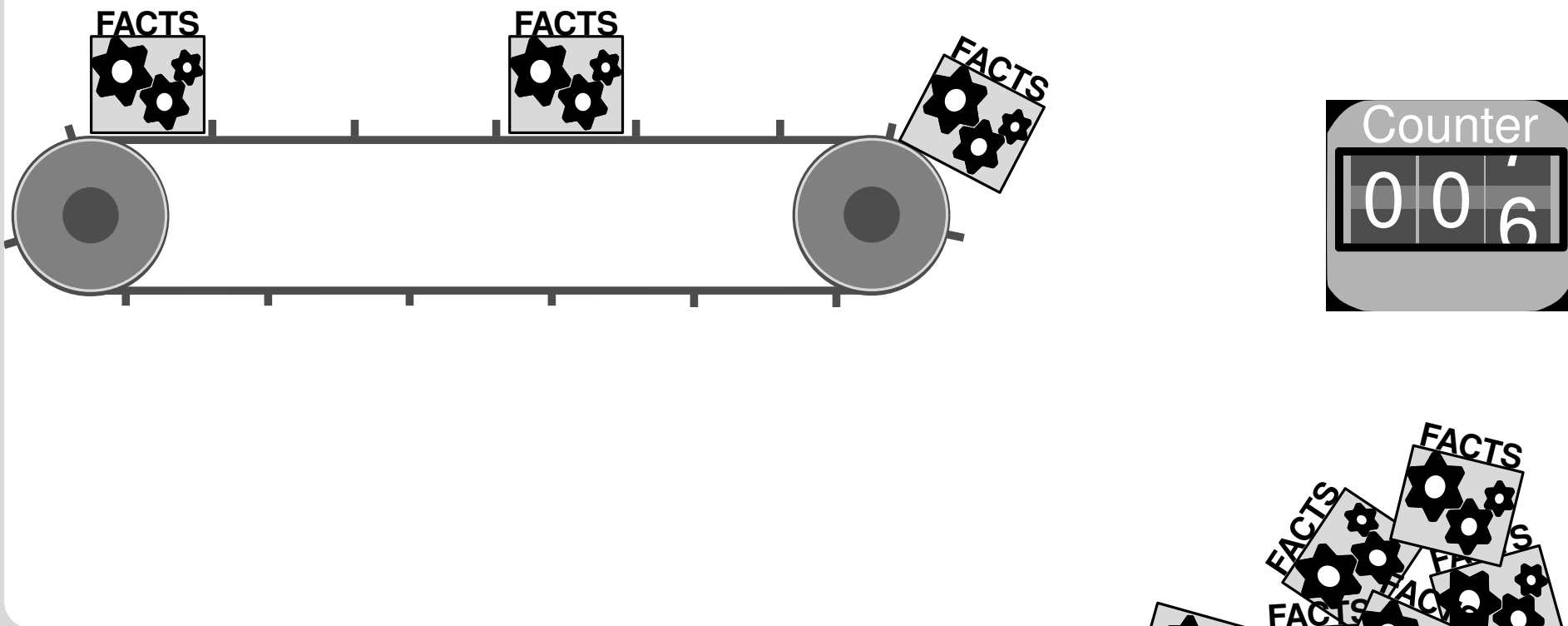
Effect of Few Flow Control Branches

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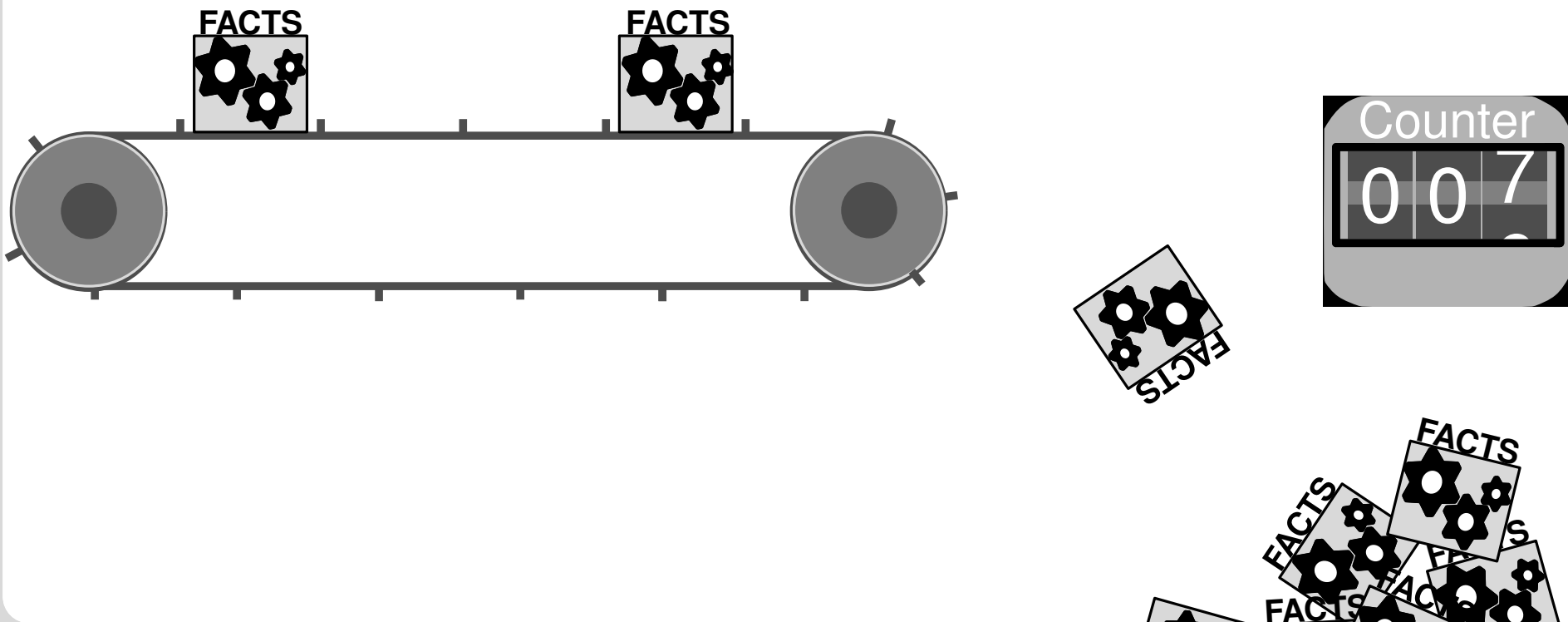
Effect of Few Flow Control Branches

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Effect of Few Flow Control Branches

Simulate load increase by a load increase factor ρ ,
Simulations with different numbers of flow controllers.



Effect of Few Flow Control Branches

Simulate load increase by a load increase factor ρ ,
Simulations with different numbers of flow controllers.

Test Data:

- IEEE instances have basically “unlimited” edge capacities
- Reduce capacities to total demand (no effect on cost and feasibility)
- Gradually increase all loads by factor ρ , or, alternatively, reduce all capacities by $1/\rho$
- Compute generation cost and required number of controllers for optimality

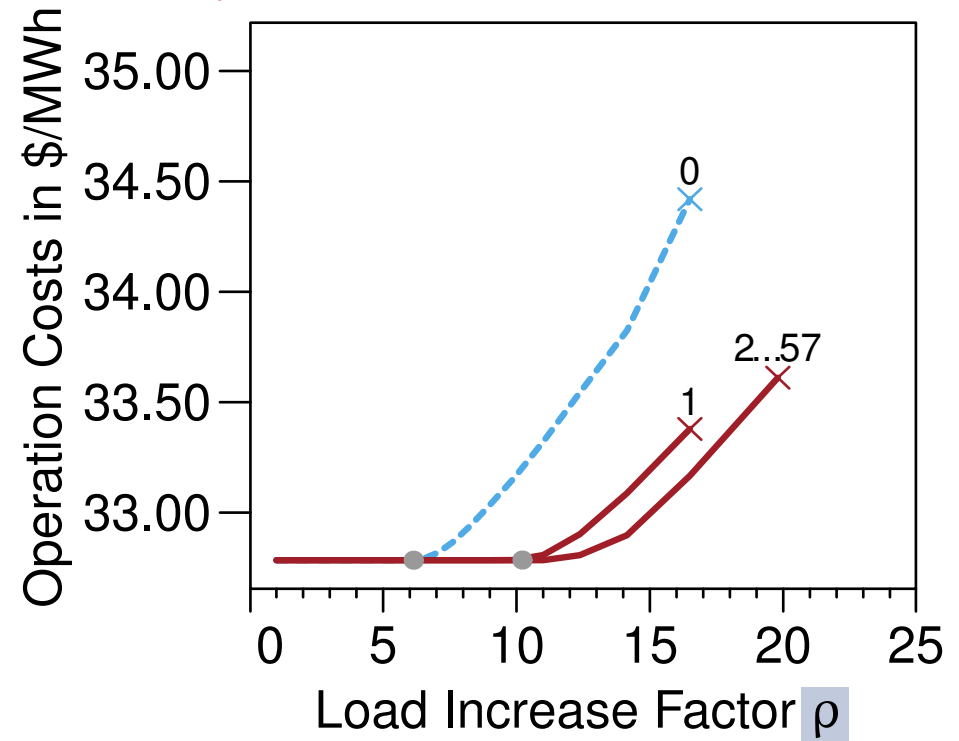
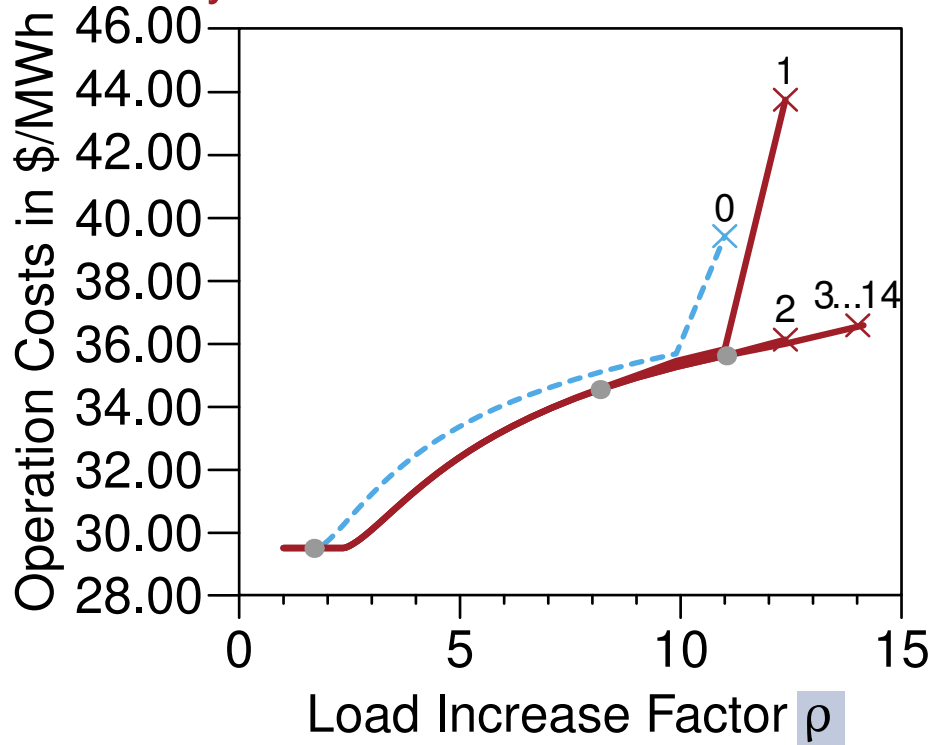
Hybrid Model Operation under Increasing Loads

case 14

case 57

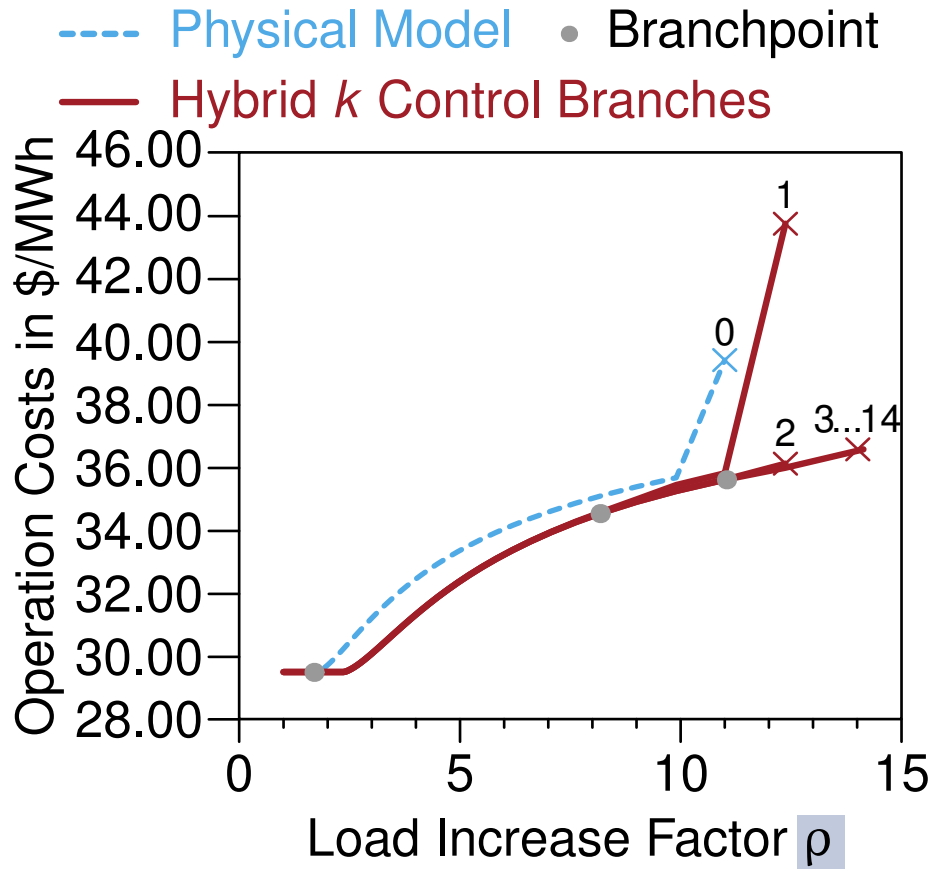
---- Physical Model • Branchpoint
 — Hybrid k Control Branches

---- Physical Model • Branchpoint
 — Hybrid k Control Branches

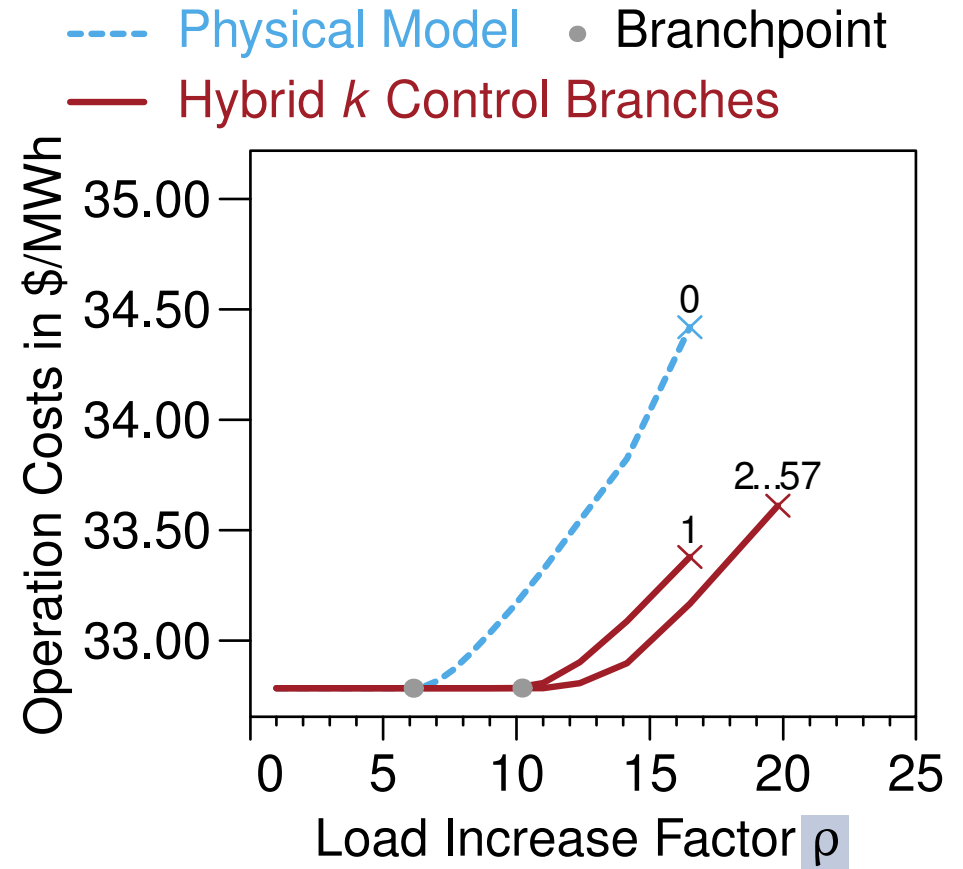


Hybrid Model Operation under Increasing Loads

case 14



case 57



Findings

Very few flow control branches extend operation point at lower cost.

Summary & Future Work

Hybrid Model = Flow Model + Physical Model

Question 1: Optimality

- How many controlled branches?
- Which branches need control?

Question 2: Cost & Operability

- Is there a positive effect on flow costs and operability?

Findings

- Often a small number of flow control branches suffices

Findings

- Extend the operation point
- Lower operation cost having only very few flow control branches

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